

Anticipating Tipping Points: Theoretical and Practical Considerations

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Institute for Advanced Study

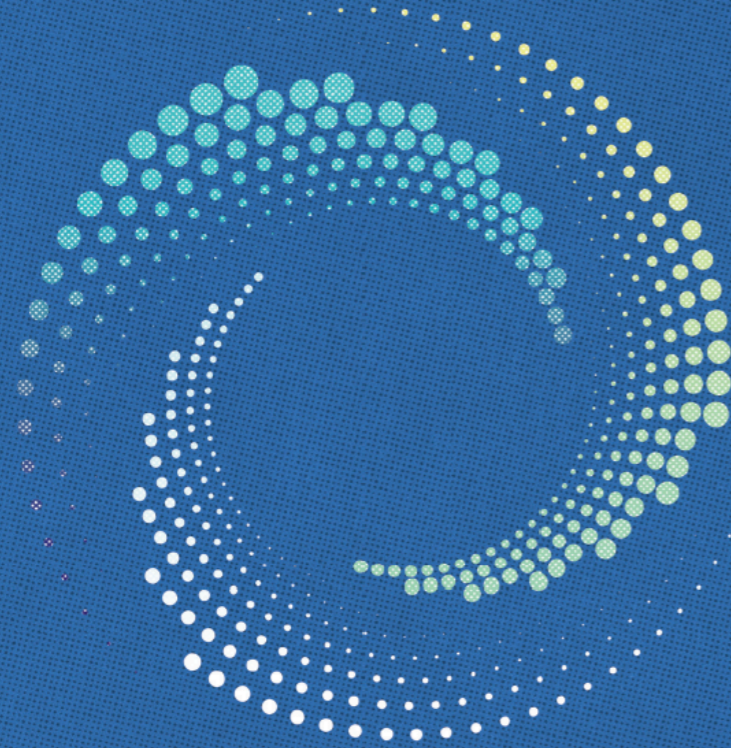
University of Amsterdam

Frontiers in Early Warning Signals Research Workshop

Kaiserslautern

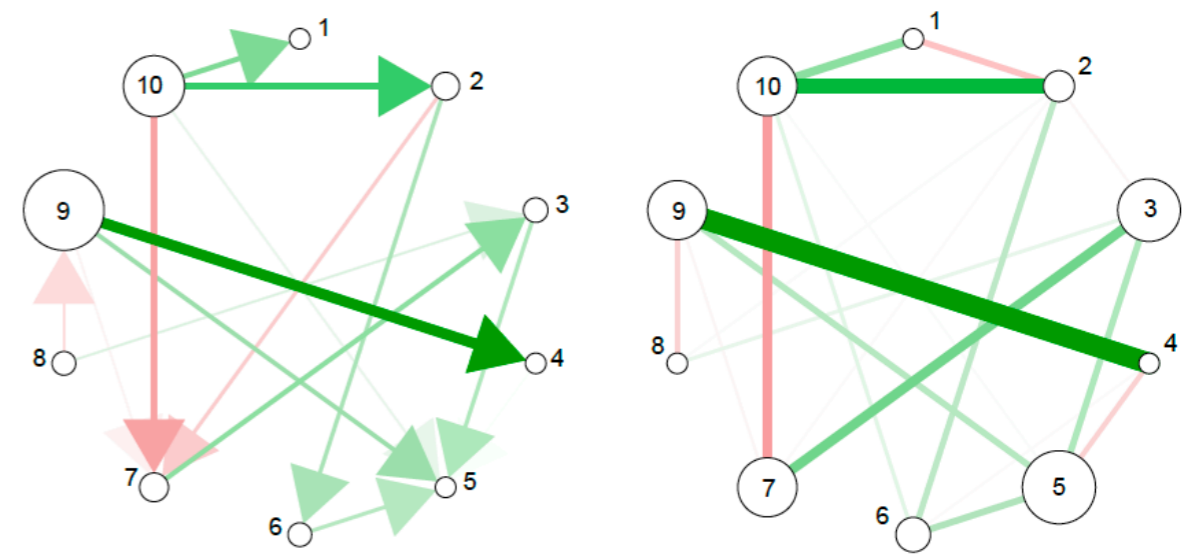
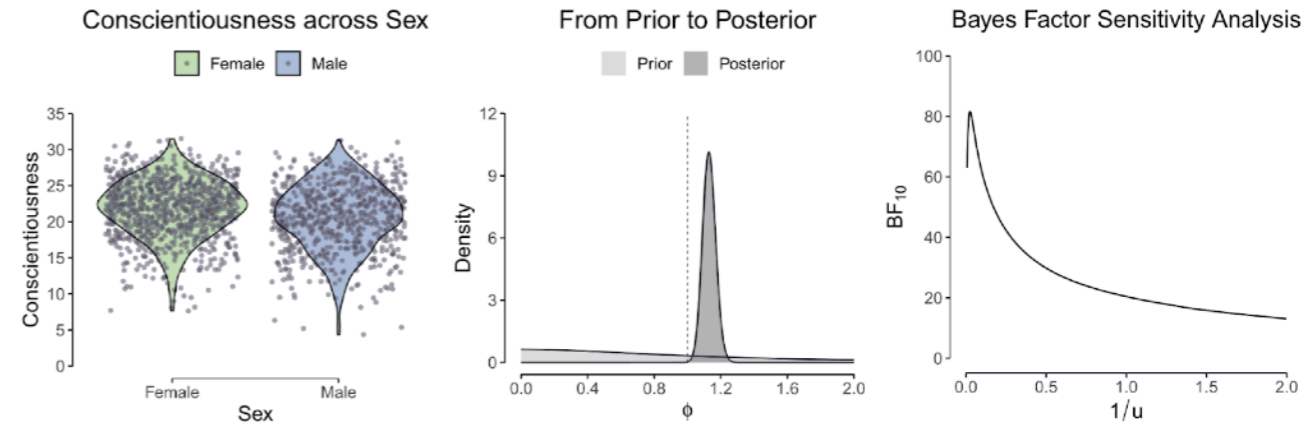
17th May, 2024

CHANGING SYSTEMS

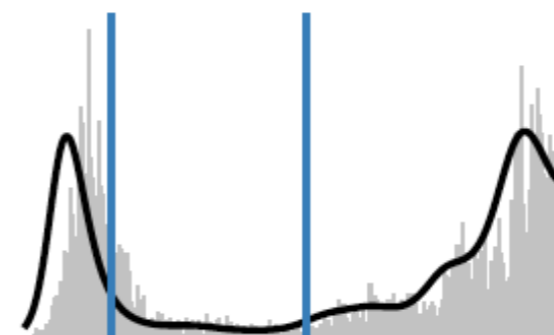


Statistical, Causal, and
Dynamical Perspectives

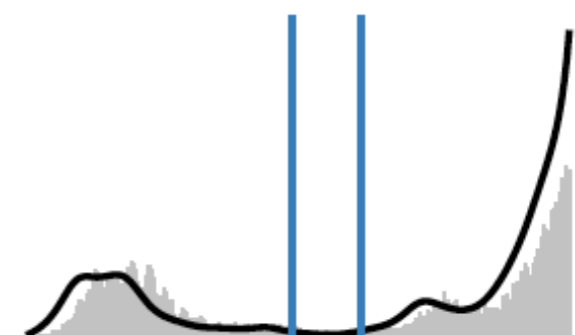
FABIAN DABLANDER



Austria



Netherlands



de Volkskrant

Opinie: Een geslaagde energietransitie begint met minder in plaats van meer



Een optimistisch klimaatverhaal kunnen we goed gebruiken, maar het moet wel kloppen

Onze leiders doen veel te weinig voor het klimaat. Daarom zijn wij nu zelf aan zet

Het Parool Vrij, Ongecensurd

Opinie: 'Er is geen koolstofbudget meer voor rijke landen, stop met koolstofgraaien'

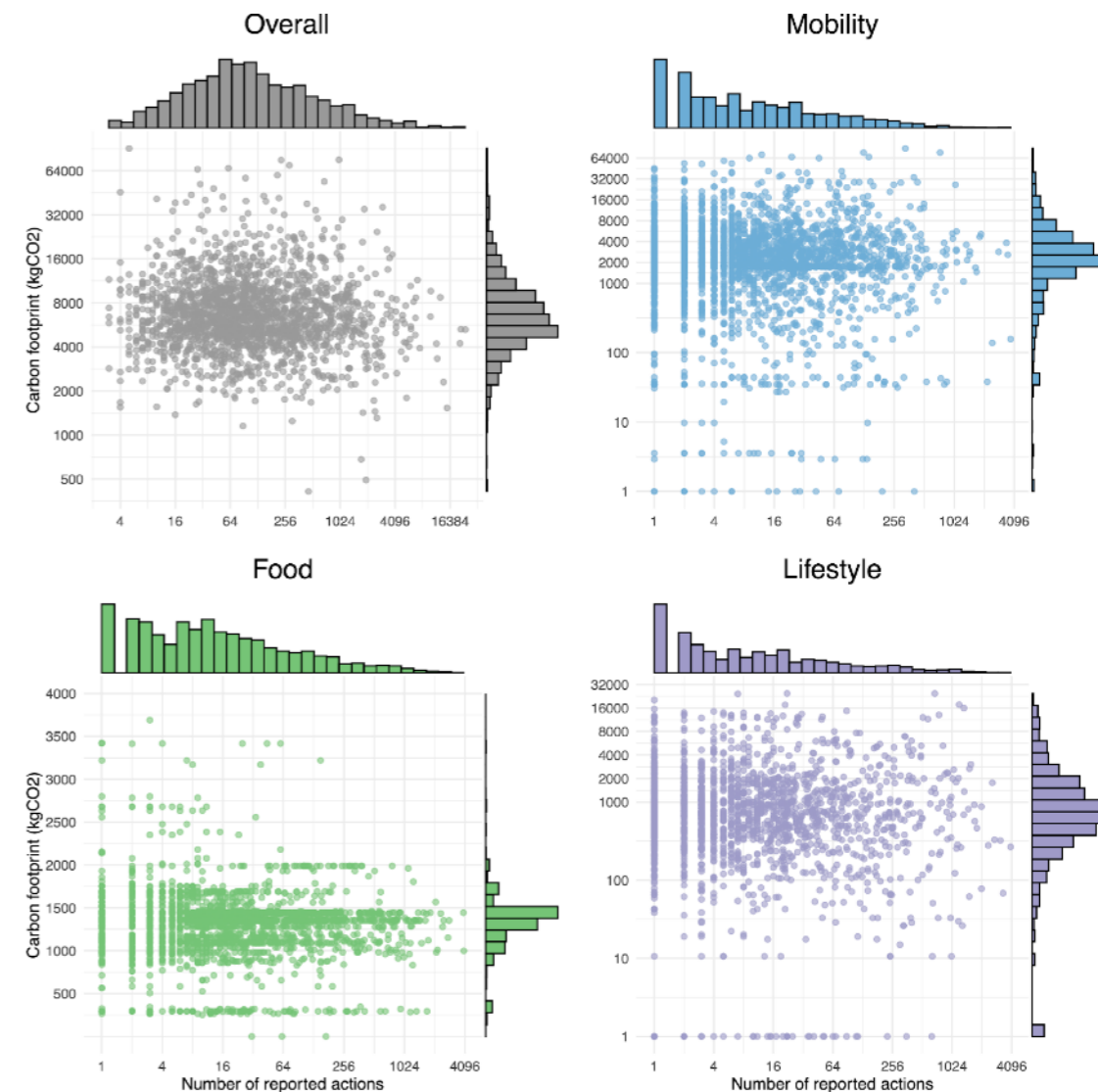
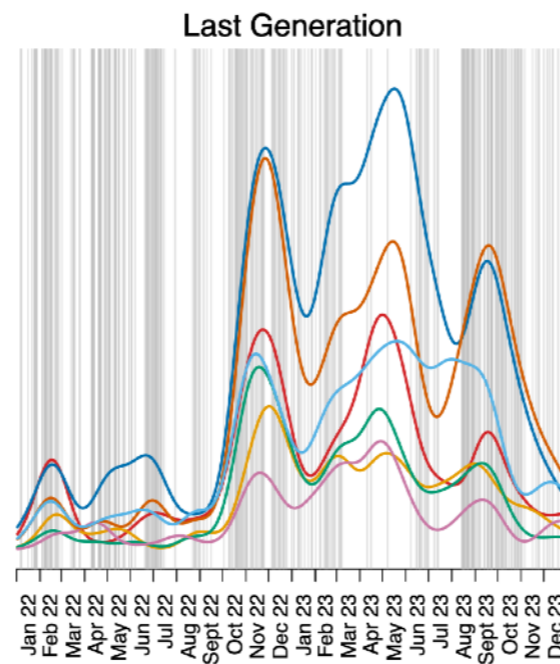
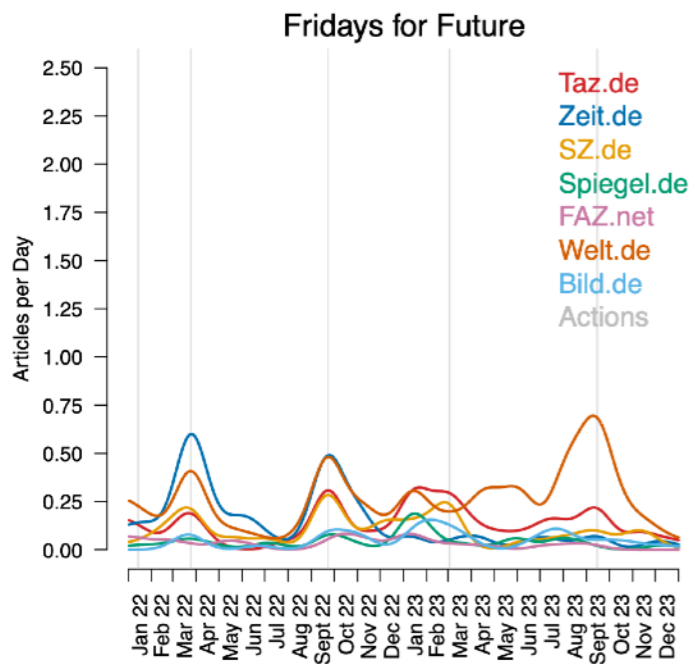
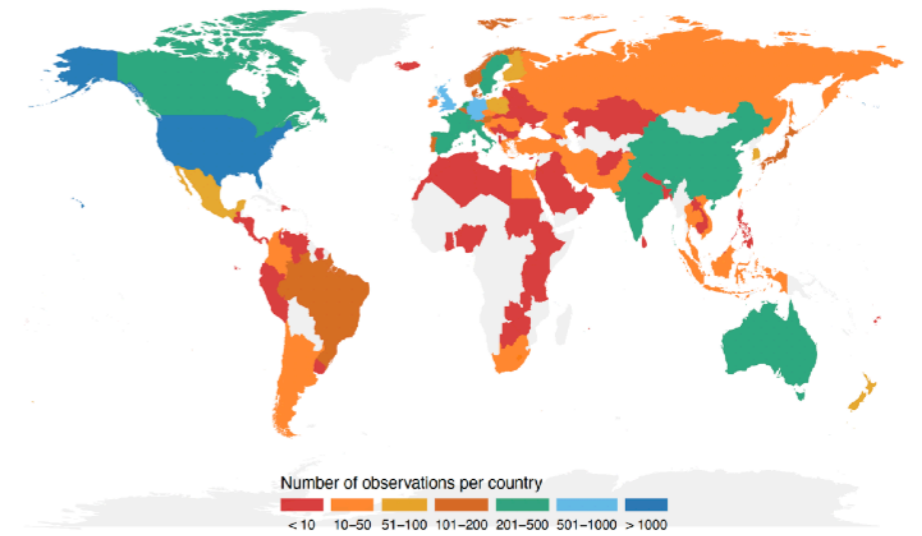
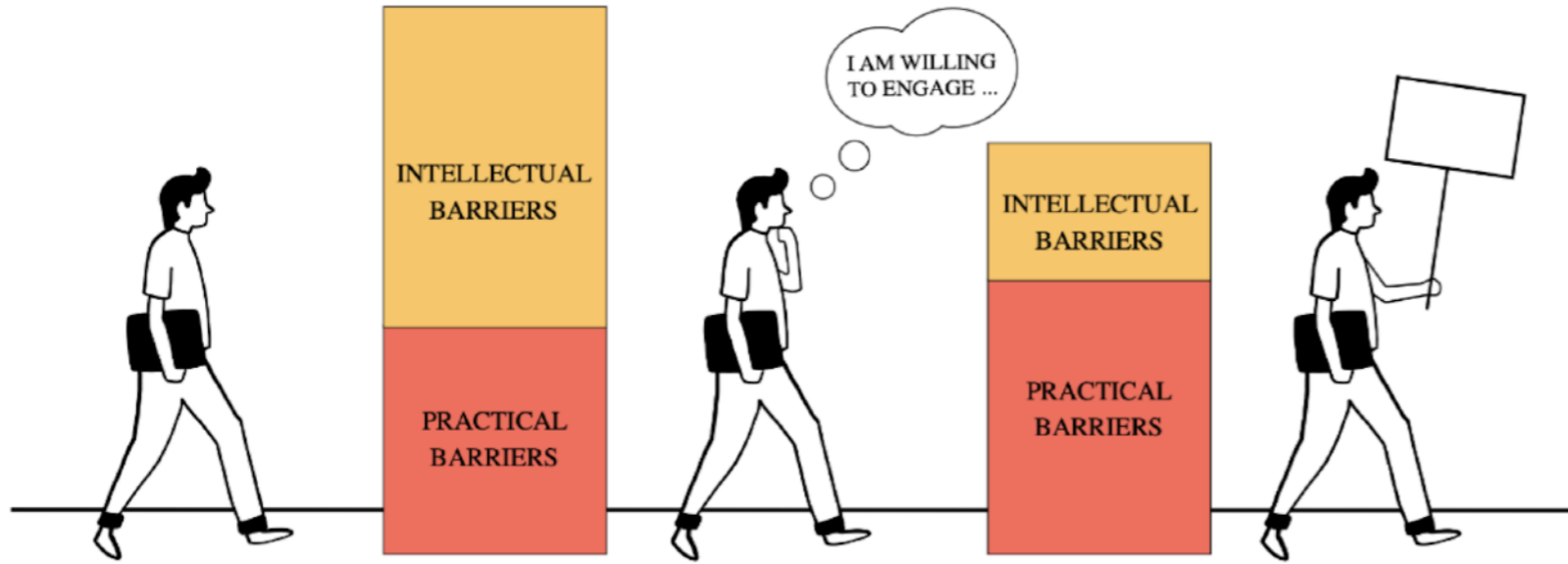
nature

Scientists skip COP28 to demand climate action at home



More than 1,000 climate scientists urge public to become activists





Barriers to climate change engagement
Effects of social movements
(Overcoming barriers) to sufficiency

Outline

A brief history

Theoretical considerations

Practical considerations



15 min

Example from Epidemiology



15 min

Conclusion & Discussion



15 min

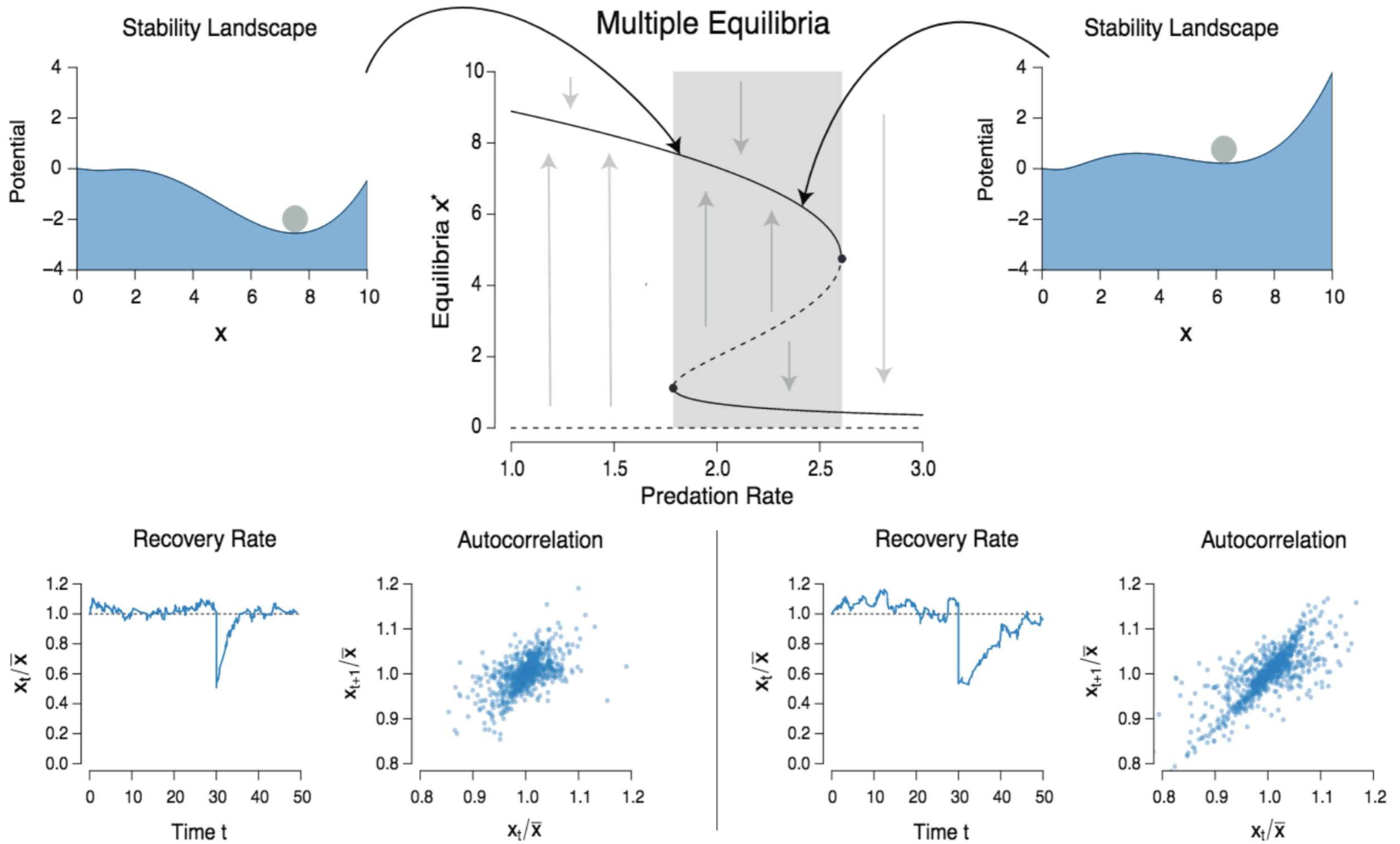
Defining tipping points for social-ecological systems scholarship—an interdisciplinary literature review

Manjana Milkoreit¹, Jennifer Hodbod^{2,11} , Jacopo Baggio³, Karina Benessaiah⁴, Rafael Calderón-Contreras⁵, Jonathan F Donges^{6,7}, Jean-Denis Mathias⁸, Juan Carlos Rocha⁷, Michael Schoon⁹ and Saskia E Werners¹⁰

“A tipping point is a threshold at which small quantitative changes in the system trigger a non-linear change process that is driven by system-internal feedback mechanisms and inevitably leads to a qualitatively different state of the system, which is often irreversible.”

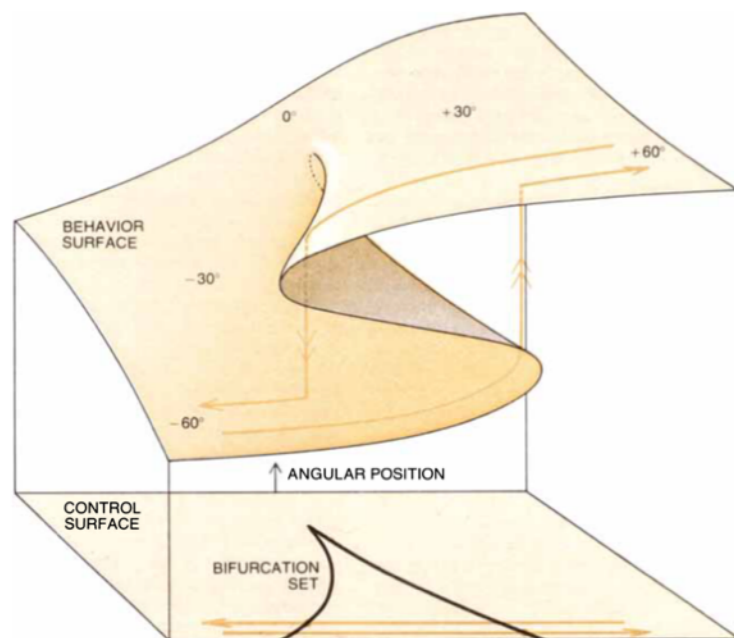
Higher Resilience

Lower Resilience



That's not new ...

- In the 1960s, René Thom developed catastrophe theory
 - Describes how (low-dimensional) systems can change suddenly
 - Popularized by Christopher Zeeman ([1976](#)), who applied it to everything
- There are a lot of key concepts in catastrophe theory:
 - Multiple stable states, critical slowing down, sudden jumps, hysteresis etc.
- However, proponents of catastrophe theory have pushed it too far
 - Catastrophe theory has been described as a great intellectual bubble
 - Zahler & Sussmann ([1977](#)) offer a prominent critique



... but it became popular again

Catastrophic shifts in ecosystems

Marten Scheffer*, Steve Carpenter†, Jiří Štřelák‡

* Department of Aquatic Ecology and Water Quality Management, Wageningen University, Wageningen, The Netherlands

† Center for Limnology, University of Wisconsin-Madison, Madison, Wisconsin, USA

‡ Center for Sustainability and the Global Environment, University of Wisconsin-Madison, Madison, Wisconsin 53706, USA

§ Department of Systems Ecology and Centre for Sustainability, Wageningen University, Wageningen, The Netherlands

|| CSIRO Sustainable Ecosystems, GPO Box 287, Canberra, ACT 2601, Australia

REVIEWS

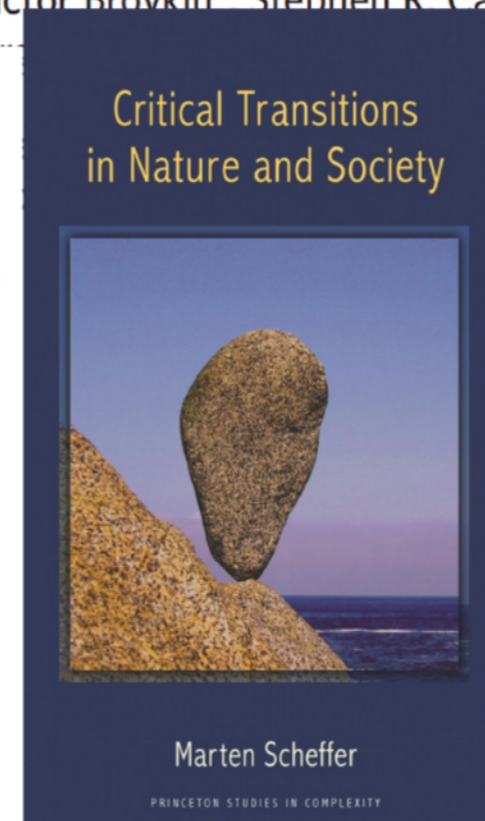
Early-warning signals for critical transitions

Marten Scheffer¹, Jordi Bascompte², William A. Brock³, Victor Brovkin⁵, Stephen R. Carpenter⁴, Vasilis Dakos¹, Egbert H. van Nes^{1,6}, E. J. van Veen¹, Neil M. Dunne⁷, S. C. Solomon⁸

Anticipating Critical Transitions

Marten Scheffer,^{1,2*} Stephen R. Carpenter,³ Timothy M. Lenton,⁴ Jordi Bascompte,⁵ William Brock,⁶ Vasilis Dakos,^{1,5} Johan van de Koppel,^{7,8} Ingrid A. van de Leemput,¹ Simon A. Levin,⁹ Egbert H. van Nes,¹ Mercedes Pascual,^{10,11} John Vandermeer¹⁰

Tipping points in complex systems may imply risks of unwanted collapse, but also opportunities for positive change. Our capacity to navigate such risks and opportunities can be boosted by combining emerging insights from two unconnected fields of research. One line of work is revealing fundamental architectural features that may cause ecological networks, financial markets, and other complex systems to have tipping points. Another field of research is uncovering generic empirical indicators of the proximity to such critical thresholds. Although sudden shifts in complex systems will inevitably continue to surprise us, work at the crossroads of these emerging fields offers new approaches for anticipating critical transitions.



Complex systems have tipping points at which they undergo abrupt transitions before they are reached. This book explores generic early-warning signals that

Published: 11 October 2001

Catastrophic shifts in ecosystems

Marten Scheffer , Steve Carpenter, Jonathan A. Foley, Carl Folke & Brian Walker

Nature **413**, 591–596 (2001) | [Cite this article](#)

39k Accesses | **4087** Citations | **101** Altmetric

LETTER  Full Access

Rising variance: a leading indicator of ecological transition

S. R. Carpenter , W. A. Brock

REVIEW

Anticipating Critical Transitions

Marten Scheffer^{1,2,*}, Stephen R. Carpenter³, Timothy M. Lenton⁴, Jordi Bascompte⁵, William Brock⁶, Vasilis Dakos^{1,5},

van de K **REPORT**

Vanderm **Early Warnings of Regime Shifts: A Whole-Ecosystem Experiment**

S. R. Carpenter^{1,*}, J. J. Cole², M. L. Pace³, R. Batt¹, W. A. Brock⁴, T. Cline¹, J. Coloso³, J. R. Hodgson⁵, J. F. Kitchell¹, D. A. Seekell³, L. Smith¹, B. Weidel¹

Methods for Detecting Early Warnings of Critical Transitions in Time Series Illustrated Using Simulated Ecological Data

Vasilis Dakos^{1,2,*}, Stephen R. Carpenter³, William A. Brock⁴, Aaron M. Ellison⁵, Vishwesh Guttal⁶,

Antho **Early Warning Signals of Ecological Transitions: Methods for Spatial Patterns**

Sonia Kéfi^{1,*}, Vishwesh Guttal², William A. Brock^{3,4}, Stephen R. Carpenter³, Valerie N. Livina⁷, David A. Seekell⁸, Marten Scheffer⁹, Egbert H. van Nes⁹, \

REPORT

Generic Indicators for Loss of Resilience Before a Tipping Point Leading to Population Collapse

Lei Dai^{1,*}, Daan Vorselen^{2,*}, Kirill S. Korolev¹, Jeff Gore^{1,†}

Published: 03 September 2009

Early-warning signals for critical transitions

Marten Scheffer , Jordi Bascompte, William A. Brock, Victor Brovkin, Stephen R. Carpenter, Vasilis Dakos, Hermann Held, Egbert H. van Nes, Max Rietkerk & George Sugihara

Nature **461**, 53–59 (2009) | [Cite this article](#)

38k Accesses | **2052** Citations | **154** Altmetric | [Metrics](#)

Published: 10 April 2013

Slower recovery in space before collapse of connected populations

Lei Dai , Kirill S. Korolev & Jeff Gore 

Nature **496**, 355–358 (2013) | [Cite this article](#)

12k Accesses | **118** Citations | **39** Altmetric | [Metrics](#)

Evaluating early-warning indicators of critical transitions in natural aquatic ecosystems

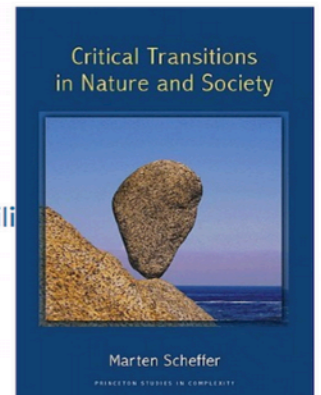
Alena Sonia Gsell^{a,b,1}, Ulrike Scharfenberger^{a,c}, Deniz Özkundakci^d, Annika Walters^e, Lars-Anders Hansson^f, Annette B. G. Janssen^{h,g}, Peeter Nöges^h, Philip C. Reid^{h,k}, Daniel E. Schindler^l, Ellen Van Donk^h, Vasilis Dakos^m, and Rita Adrian^{a,c}

Turning back from the brink: Detecting an impending regime shift in time to avert it

Reinette Biggs^{a,1}, Stephen R. Carpenter^{a,2}, and William A. Brock^b

Quantifying resilience of humans and other animals

Marten Scheffer^{a,1}, J. Elizabeth Bolhuis^b, Denny Borsboom^c, Timothy G. Buchman^d, Sanne M. W. Gijzel^{a,e}, Dave Goulson^f, Jan E. Kammenga^g, Bas Kemp^b, Ingrid A. van de Leemput^g, Simon Levin^h, Carmel Mary Martinⁱ, René J. F. Melis^e, Egbert H. van Nes^a, L. Michael Romer^d, and Marcel G. M. Olde Rikkert^e



Published: 08 September 2010

Early warning signals of extinction in deteriorating environments

John M. Drake  & Blaine D. Griffen

Nature **467**, 456–459 (2010) | [Cite this article](#)

5700 Accesses | **307** Citations | **40** Altmetric | [Metrics](#)

Waiting time to infectious disease emergence

Christopher J. Dibble¹, Eamon B. O’Dea^{1,2}, Andrew W. Park^{1,2} and John M. Drake^{1,2}

Theory of early warning signals of disease emergence and leading indicators of elimination

Suzanne M. O’Regan · John M. Drake






PERSPECTIVE

The statistics of epidemic transitions

John M. Drake ^{1,2,*}, Tobias S. Brett^{1,2}, Shiyang Chen³, Bogdan I. Epureanu ^{3,4}, Matthew J. Ferrari⁵, Éric Marty^{1,2}, Paige B. Miller ^{1,2}, Eamon B. O’Dea ^{1,2}, Suzanne M. O’Regan⁶, Andrew W. Park ^{1,2}, Pejman Rohani ^{1,2}

RESEARCH ARTICLE

Detecting critical slowing down in high-dimensional epidemiological systems

Tobias Brett ^{1,2,*}, Marco Ajelli^{3,4}, Quan-Hui Liu ^{3,5}, Mary G. Krauland⁶, John J. Grefenstette ⁶, Willem G. van Panhuis^{7,8}, Alessandro Vespignani^{3,9}, John M. Drake ^{1,2}, Pejman Rohani ^{1,2,10}

Transient indicators of tipping points in infectious diseases

Suzanne M. O’Regan^{1,†}, Eamon B. O’Dea^{2,3,†}, Pejman Rohani^{2,3,4} and John M. Drake^{2,3}

Estimating the distance to an epidemic threshold

Eamon B. O’Dea^{1,2}, Andrew W. Park^{3,4} and John M. Drake^{2,3}

Anticipating the emergence of infectious diseases

Tobias S. Brett^{1,2}, John M. Drake^{1,2} and Pejman Rohani^{1,2,3}

Early warning signals of malaria resurgence in Kericho, Kenya

Mallory J. Harris^{1,3}, Simon I. Hay^{4,5} and John M. Drake^{1,2}


RESEARCH ARTICLE

Anticipating epidemic transitions with imperfect data

Tobias S. Brett^{1,2,*}, Eamon B. O’Dea^{1,2}, Éric Marty¹, Paige B. Miller^{1,2}, Andrew W. Park^{1,2,3}, John M. Drake^{1,2}, Pejman Rohani^{1,2,3}

RESEARCH ARTICLE

Dynamical footprints enable detection of disease emergence

Tobias S. Brett ^{1,2,*}, Pejman Rohani^{1,2,3}

Slowing Down of Recovery as Generic Risk Marker for Acute Severity Transitions in Chronic Disease

Marcel G. M. Olde Rikkert, MD, PhD¹; Vasilis Dakos, PhD²; Timothy G. Buchman, PhD, MD³; Rob de Boer, PhD⁴; Leon Glass, PhD⁵; Angélique O. J. Cramer, PhD⁶; Simon Levin, PhD⁷; Egbert van Nes, PhD⁸; George Sugihara, PhD⁹; Michel D. Ferrari, MD, PhD¹⁰; Else A. Tolner, PhD¹¹; Ingrid van de Leemput, MSc⁸; Joep Lagro, MD, PhD¹¹; René Melis, MD, PhD¹; Marten Scheffer¹

Critical Fluctuations as an Early-Warning Signal for Sudden Gains and Losses in Patients Receiving Psychotherapy for Mood Disorders



Merlijn Olthof¹, Fred Hasselman^{1,2}, Guido Strunk^{3,4,5}

RESEARCH ARTICLE

Open Access

Early warning signals in psychopathology: what do they tell?

Marieke J. Schreuder^{1*}, Catharina A. Hartman¹, Sandip V. George¹, Claudia Menne-Lothmann², Jeroen [unclear]^{3,4}, Bart P. F. [unclear]^{5,6,7,8,9,10}

cambridge.org/psm

Invited Review

Cite this article: Wichers M, Schreuder MJ, Goekoop R, Groen RN (2018). Can we predict the direction of sudden shifts in symptoms? Transdiagnostic implications from a complex systems perspective on psychopathology. *Psychological Medicine* 49, 380–387. <https://doi.org/10.1017/S0033291718000000>

Can we predict the direction of sudden shifts in symptoms? Transdiagnostic implications from a complex systems perspective on psychopathology

Marieke Wichers¹, Marieke J. Schreuder¹, Rutger Goekoop² and Robin N. Groen¹

¹University of Groningen, University Medical Center Groningen, Department of Psychiatrie, Interdisciplinary Center Psychopathology and Emotion Regulation (ICPE), Groningen, The Netherlands and ²Department of Mood Disorders, Parnassia Group, PsyQ, The Hague, The Netherlands

Critical slowing down as early warning for the onset and termination of depression

Ingrid A. van de Leemput^{a,1,2}, Marieke Wichers^{b,1}, Angélique O. J. Cramer^c, Denny Borsboom^c, Francis Tuerlinckx^d, Peter Kuppens^{d,e}, Egbert H. van Nes^a, Wolfgang Viechtbauer^b, Erik J. Giltay^f, Steven H. Aggen^g, Catherine Derom^{h,i}, Kenneth S. Kendler^{g,k}, Han L. J. van der Maas^c, Michael C. Neale^g, Frenk Peeters^b, Evert Thiery^l, and Marten Scheffer^a

Clinical Psychological Science
1–11
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DOI: 10.1177/216770261986596
www.psychologicalscience.org/



Measurement of Dynamical Resilience Indicators Improves the Prediction of Recovery Following Hospitalization in Older Adults

Sanne M.W. Gijzel MD^{a,b}, Jerrald Rector PhD^a, Fokke B. van Meulen PhD^a, Rolinka Schim van der Loeff MSc^a, Ingrid A. van de Leemput PhD^b, Marten Scheffer PhD^b, Marcel G.M. Olde Rikkert MD, PhD^a, René J.F. Melis MD, PhD^{a,*}

^aDepartment of Geriatrics, Radboud Institute for Health Sciences, Radboud University Medical Center, Nijmegen, the Netherlands
^bDepartment of Environmental Sciences, Wageningen University, Wageningen, the Netherlands

Psychother Psychosom 2016;85:114–116

DOI: [10.1159/000441458](https://doi.org/10.1159/000441458)

Critical Slowing Down as a Personalized Early Warning Signal for Depression

Early Warning Signals Based on Momentary Affect Dynamics can Expose Nearby Transitions in Depression: A Confirmatory Single-Subject Time-Series Study

Marieke Wichers, Arnout C. Smit, and Evelien Snippe

University of Groningen, University Medical Center Groningen (UMCG), Dept. of Psychiatry, Interdisciplinary Center Psychopathology and Emotion regulation (ICPE), Groningen, The Netherlands

Tipping elements in the Earth's climate system

Timothy M. Lenton^{*†}, Hermann Held[‡], Elmar Kriegler^{‡§}, Jim W. Hall[¶], Wolfgang Lucht[‡], Stefan Rahmstorf[‡], and Hans Joachim Schellnhuber^{†‡||**}

Slowing down as an early warning signal for abrupt climate change

Vasilis Dakos^{*}, Marten Scheffer^{*†}, Egbert H. van Nes^{*}, Victor Brovkin^{‡§}, Vladimir Petoukhov[‡], and Hermann Held[‡]

ORIGINAL PAPER | [Open Access](#) | Published: 29 May 2013

Early warning signals of simulated Amazon rainforest dieback

[Chris A. Boulton](#) , [Peter Good](#) & [Timothy M. Lenton](#)

Theoretical Ecology **6**, 373–384 (2013) | [Cite this article](#)

3510 Accesses | **24** Citations | **4** Altmetric | [Metrics](#)

The tipping points and early warning indicators for Pine Island Glacier, West Antarctica

Sebastian H. R. Rosier ¹, Ronja Reese ², Jonathan F. Donges ^{2,3}, Jan De Rydt ¹, G. Hilmar Gudmundsson ¹, and Ricarda Winkelmann ^{2,4}

Review Article | Published: 29 July 2021

Past abrupt changes, tipping points and cascading impacts in the Earth system

[Victor Brovkin](#) , [Edward Brook](#), [John W. Williams](#), [Sebastian Bathiany](#), [Timothy M. Lenton](#), [Michael Barton](#), [Robert M. DeConto](#), [Jonathan F. Donges](#), [Andrey Ganopolski](#), [Jerry McManus](#), [Summer Praetorius](#), [Anne de Vernal](#), [Ayako Abe-Ouchi](#), [Hai Cheng](#), [Martin Claussen](#), [Michel Crucifix](#), [Gilberto Gallopín](#), [Virginia Iglesias](#), [Darrell S. Kaufman](#), [Thomas Kleinen](#), [Fabrice Lambert](#), [Sander van der Leeuw](#), [Hannah Liddy](#), [Marie-France Loutre](#), [David McGee](#), [Kira Rehfeld](#), [Rachael Rhodes](#), [Alistair W. R. Seddon](#), [Martin H. Trauth](#), [Lilian Vanderveken](#) & [Zicheng Yu](#) -Show fewer authors

Published: 19 June 2011

Early warning of climate tipping points

[Timothy M. Lenton](#) 

Nature Climate Change **1**, 201–209 (2011) | [Cite this article](#)

6849 Accesses | **365** Citations | **130** Altmetric | [Metrics](#)

[Open Access](#) | Published: 08 December 2014

Early warning signals of Atlantic Meridional Overturning Circulation collapse in a fully coupled climate model

[Chris A. Boulton](#) , [Lesley C. Allison](#) & [Timothy M. Lenton](#)

Nature Communications **5**, Article number: 5752 (2014) | [Cite this article](#)

9679 Accesses | **33** Citations | **136** Altmetric | [Metrics](#)

Article | Published: 05 August 2021

Observation-based early-warning signals for a collapse of the Atlantic Meridional Overturning Circulation

[Niklas Boers](#) 

Nature Climate Change **11**, 680–688 (2021) | [Cite this article](#)

6416 Accesses | **4531** Altmetric | [Metrics](#)

RESEARCH ARTICLE

Critical slowing down suggests that the western Greenland Ice Sheet is close to a tipping point

 [Niklas Boers](#) and  [Martin Rypdal](#)

Anticipating Critical Transitions in Psychological Systems Using Early Warning Signals: Theoretical and Practical Considerations

Fabian Dablander¹, Anton Pichler^{2, 3}, Arta Cika⁴, and Andrea Bacilieri^{2, 5}

¹ Department of Psychological Methods, University of Amsterdam

² Institute for New Economic Thinking at the Oxford Martin School, University of Oxford

³ Complexity Science Hub Vienna, Vienna, Austria

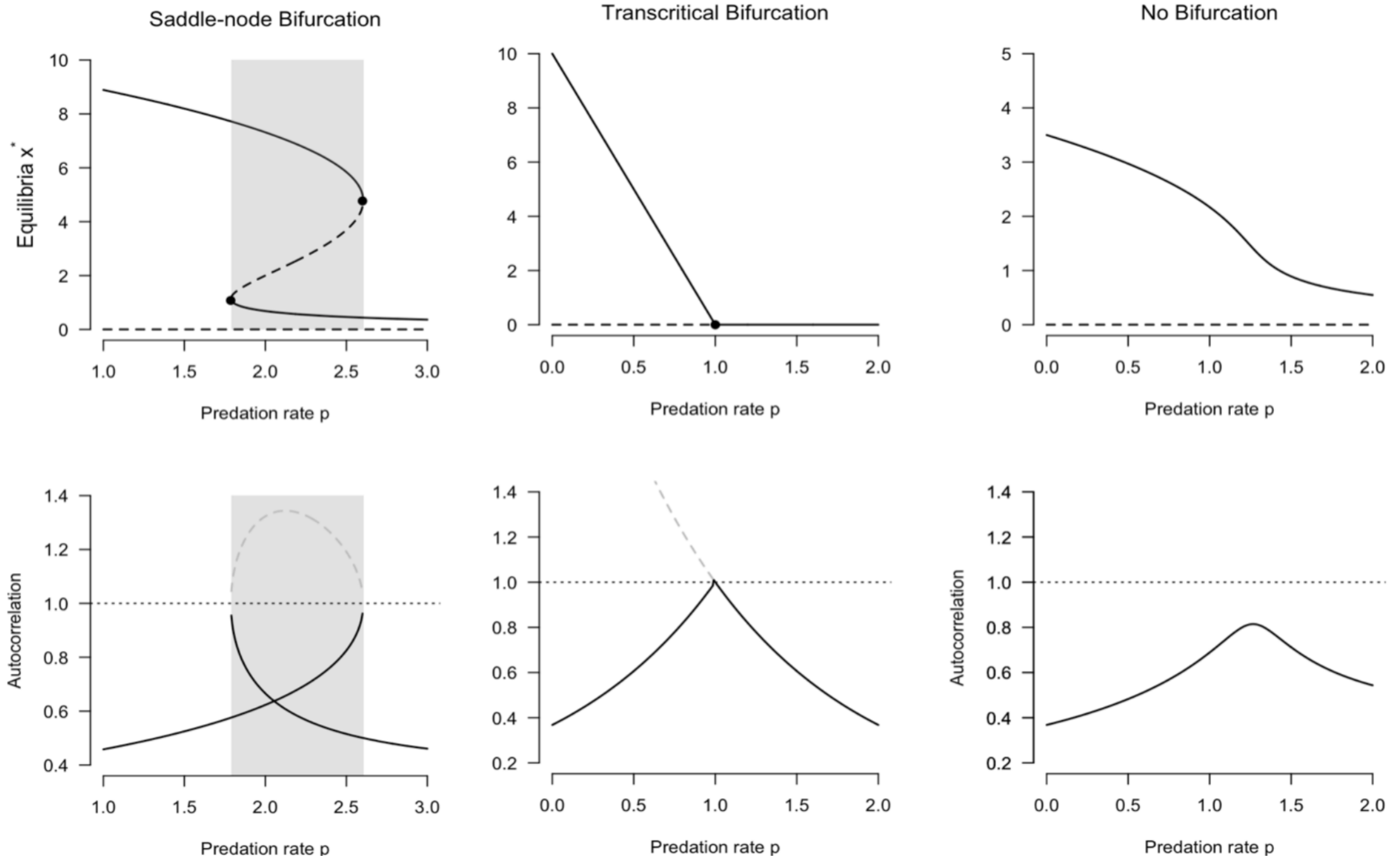
⁴ Department of Engineering Science, University of Oxford

⁵ Smith School of Enterprise and Environment, University of Oxford

Theoretical considerations

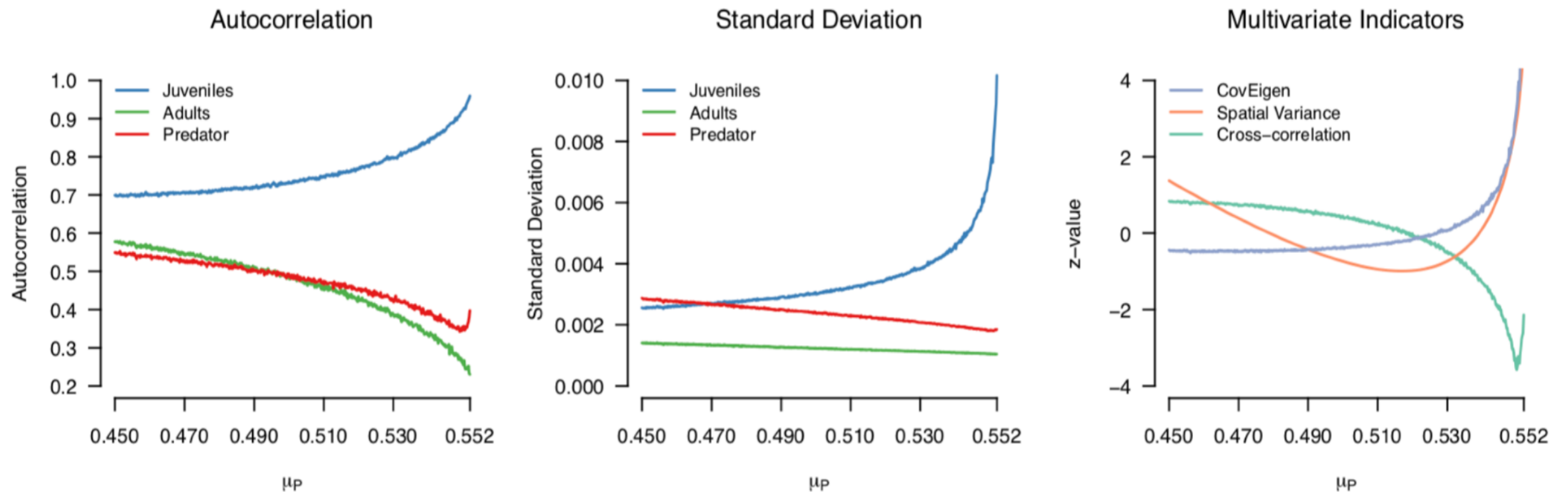
EWS without critical transitions	Critical transitions without EWS
EWS can occur prior to smooth transitions between stable states (Drake & Griffen, 2010; Kéfi et al., 2013).	Strong external perturbations can lead to transitions without EWS (Ditlevsen & Johnsen, 2010; van Nes et al., 2016).
EWS can occur when there is no transition (e.g., Wagner & Eisenman, 2015).	EWS may not occur prior to critical transitions in systems with nonsmooth potentials (Hastings & Wysham, 2010). Not all variables in a system generally express EWS equally strongly or at all (Boerlijst et al., 2013; Patterson et al., 2021). EWS may not occur under correlated or extrinsic noise (Dakos, van Nes, et al., 2012; O'Regan & Burton, 2018; Qin & Tang, 2018).

EWS prior to non-catastrophic transitions



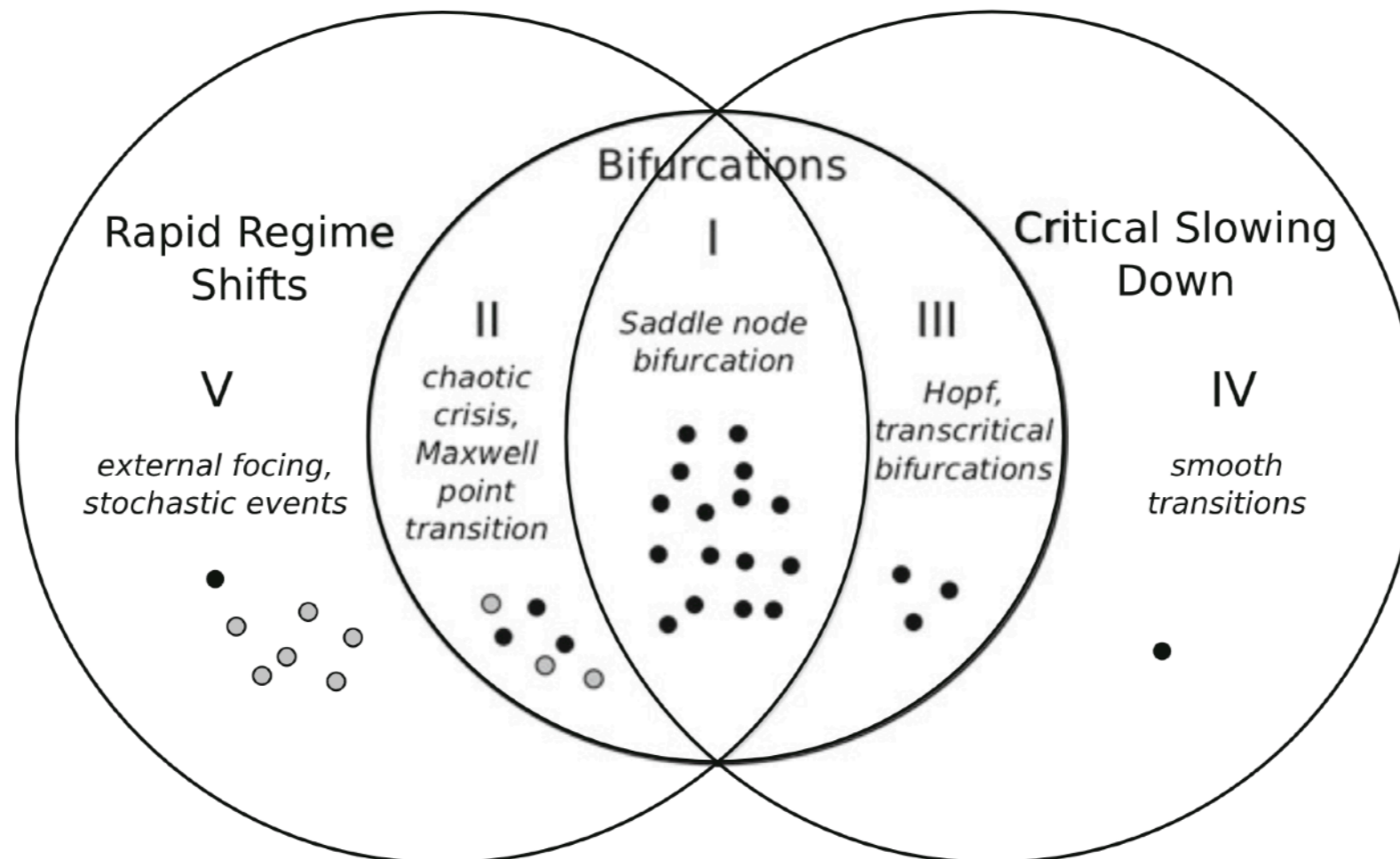
EWS not in all variables

- Not all variables express critical slowing down equally strongly or at all
- Boerlijst et al. ([2013](#)) study a staged predator-prey system
 - Predator preys on adult prey but not on juvenile prey
 - $\mu \sim 0.553$ is the bifurcation point for which the predators collapse



Interim conclusion II

- To use EWS sensibly, we need to have a good understanding of the system
 - Some vague references to “complex systems” will not do
- Finding that EWS rise **does not** mean that a tipping point is near
 - Need independent evidence of a tipping point, then EWS potentially useful

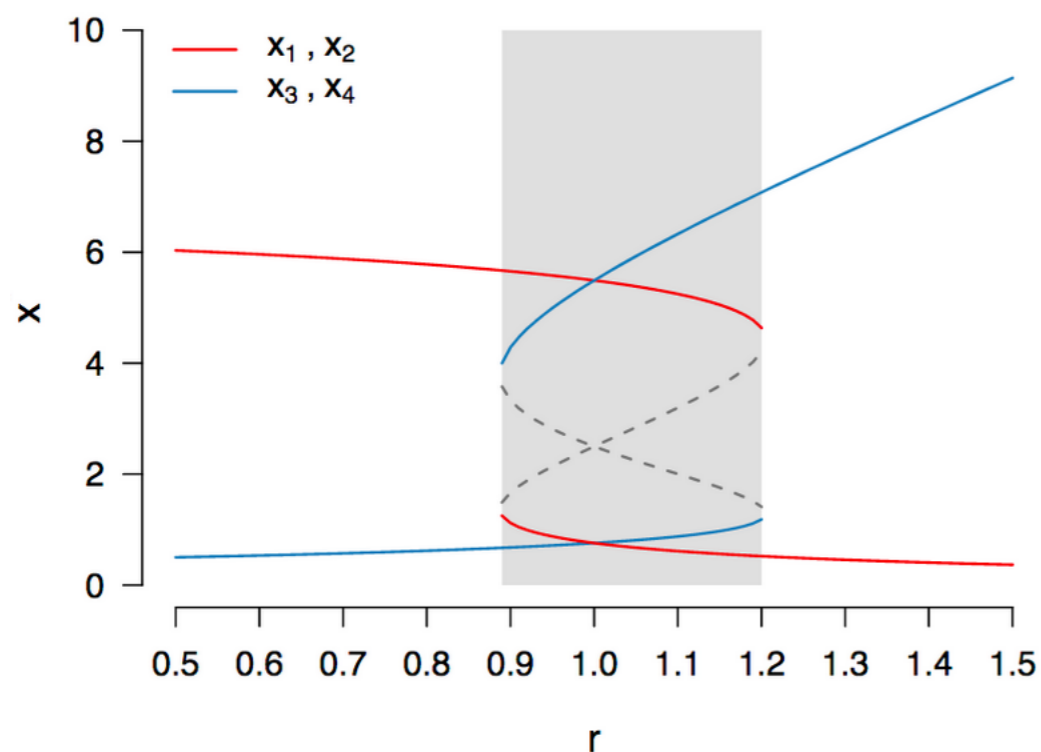


Practical considerations

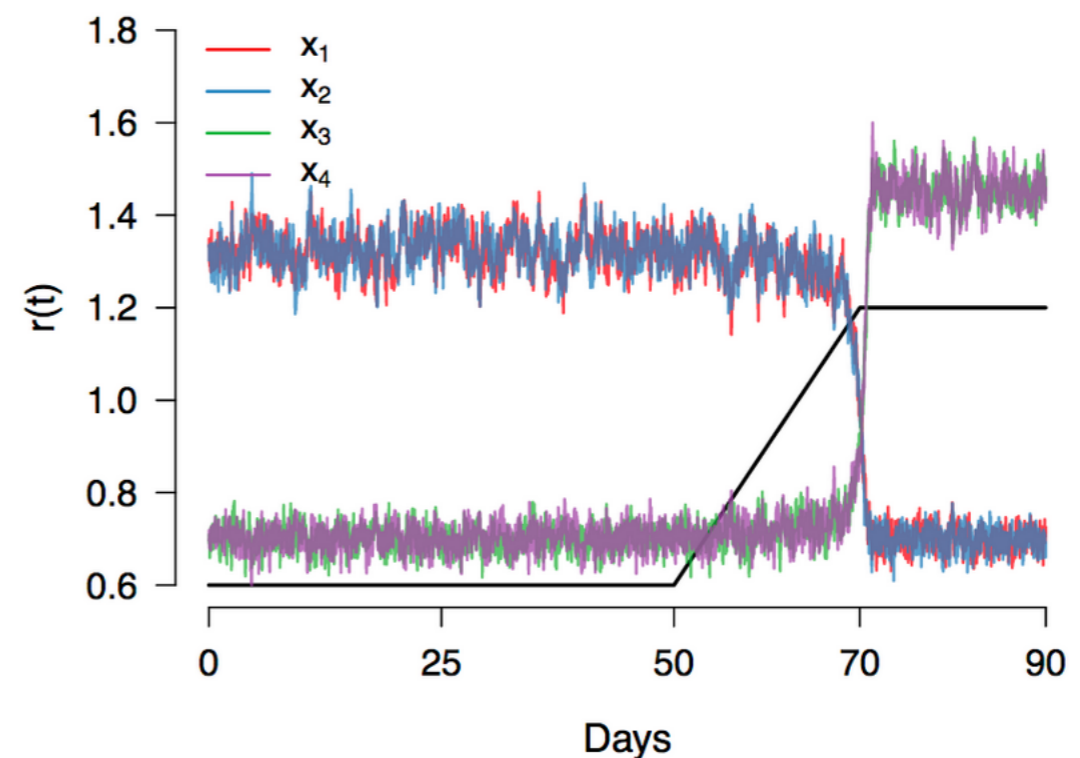
EWS performance in simulation

- EWS as online-monitoring tool for systems
 - Signal potential bad transition → intervene to prevent transition
 - Signal potential good transition → intervene to bring about transition
- Difficult statistical challenge!
 - Need to correctly estimate increasing EWS (stationarity violation)
 - Need to adequately test increase against baseline (not all EWS)

Bifurcation Diagram



Example Time Series and $r(t)$

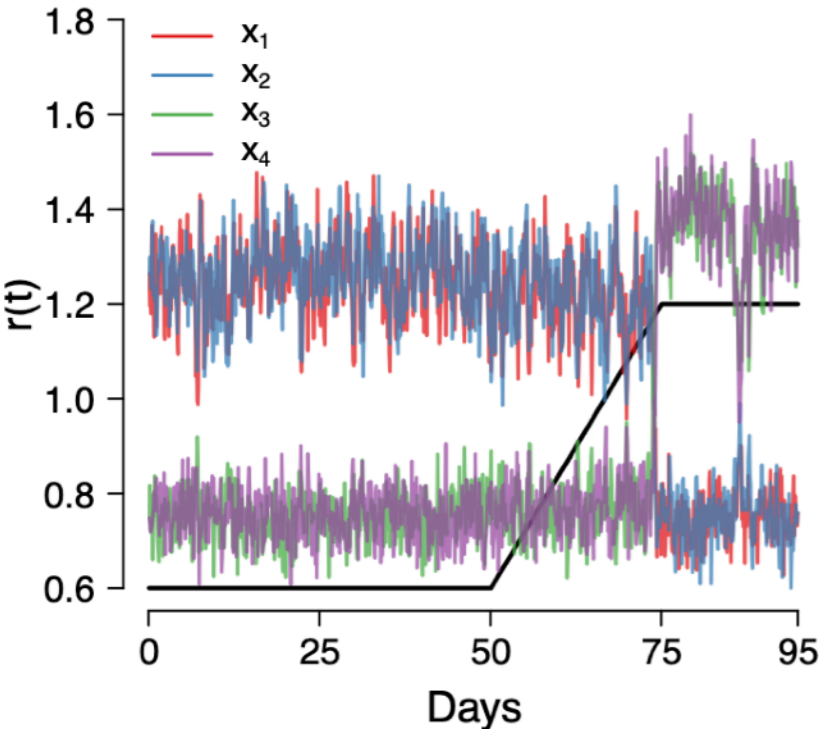


EWS performance in simulation

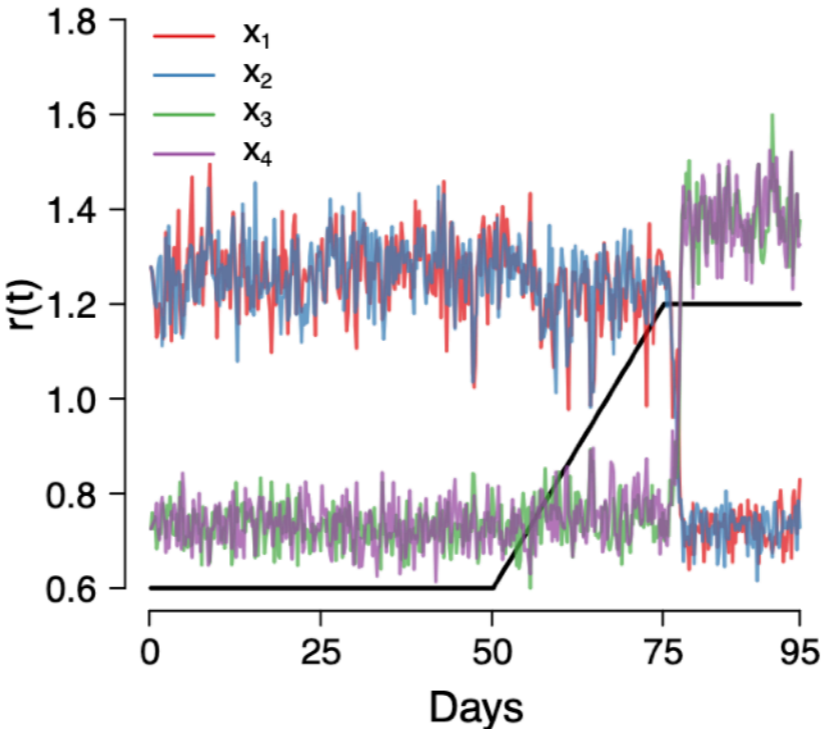
Early Warning Indicator	Source
Autocorrelation and Variance	Scheffer et al. (2009)
Skewness and Kurtosis	Guttal and Jayaprakash (2008)
Cross-correlation	Dakos et al. (2010)
Dominant eigenvalue of covariance matrix	Chen et al. (2019)
Spatial-Variance, Spatial-Kurtosis, and Spatial-Skewness	Kéfi et al. (2014)
Parameter	Values
<i>Uncontrollable</i>	
Noise intensity σ_ε	4, 6, 8, 10
Transition Period	10, 25, 50 days
<i>Controllable</i>	
Sampling Frequency	1x, 5x, 10x per day
Baseline	25, 50, 100 days
Rolling Window Size	10, 25, 50 days

EWS performance in simulation

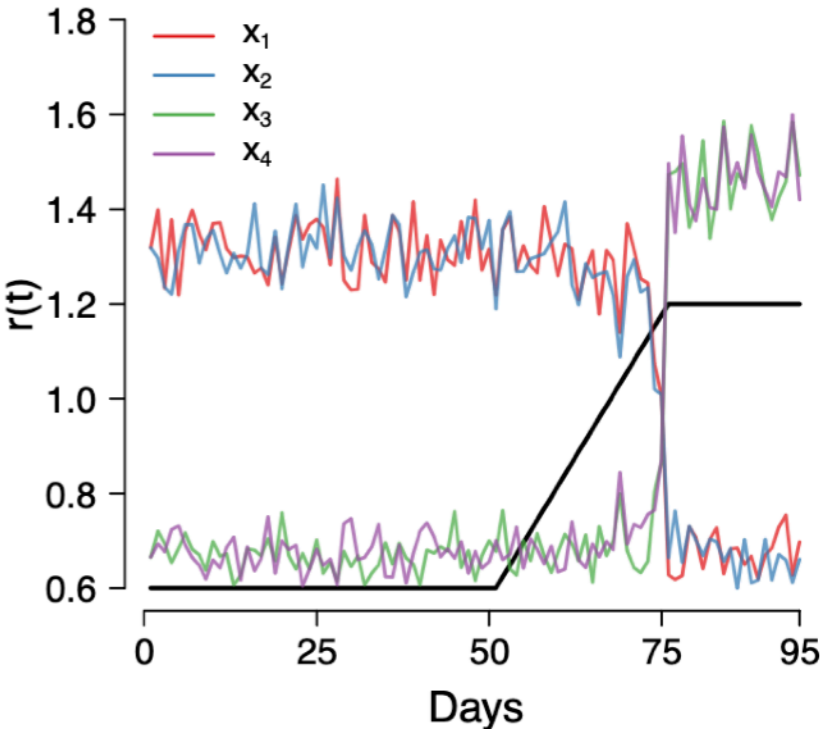
Sampling 10 x Day and $\sigma_\epsilon = 10$



Sampling 5 x Day and $\sigma_\epsilon = 8$



Sampling 1 x Day and $\sigma_\epsilon = 6$

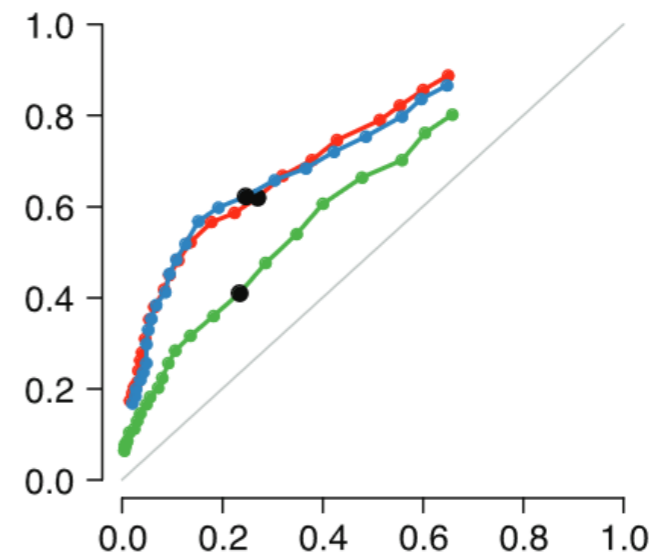
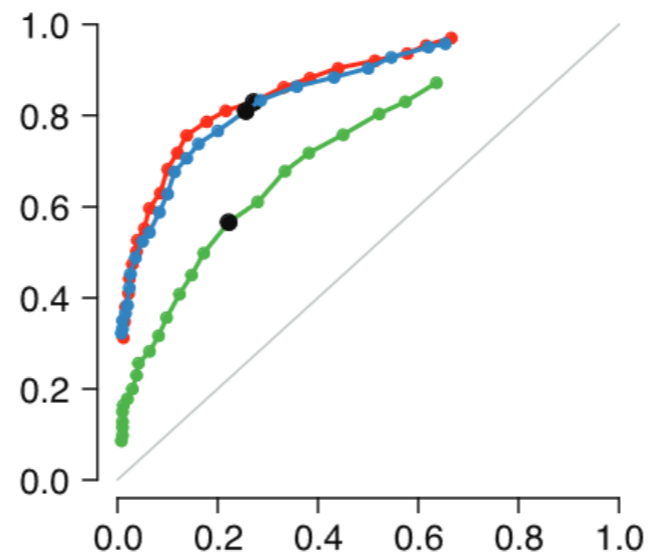
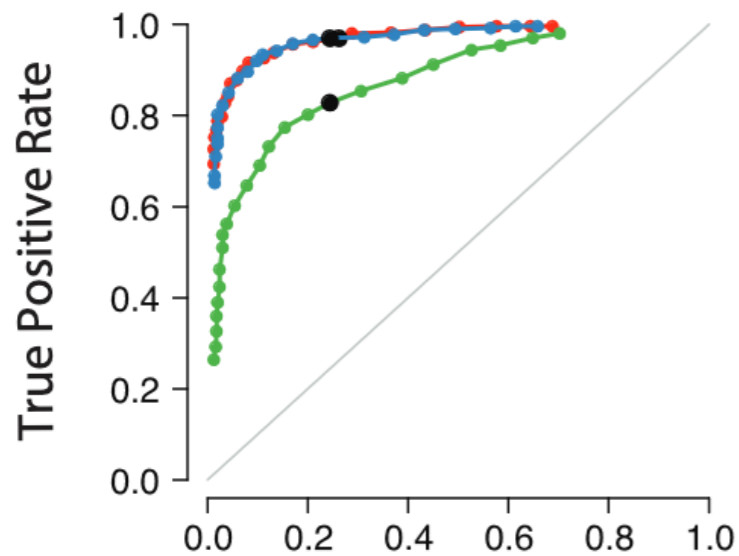


Sampling Frequency — 10x Day — 5x Day — 1x Day

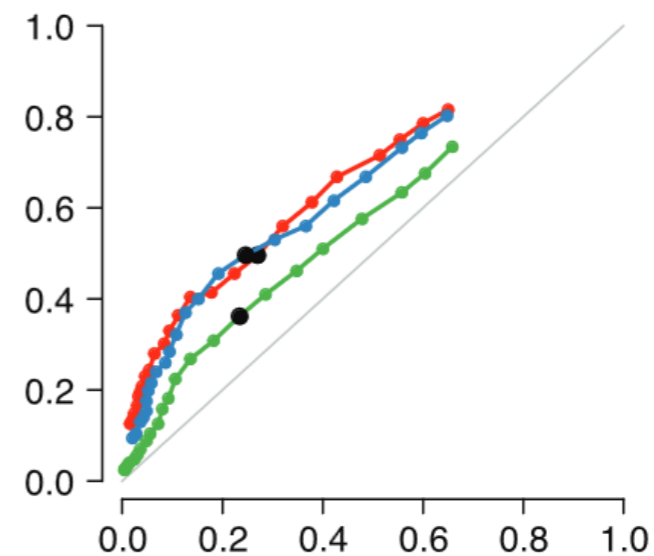
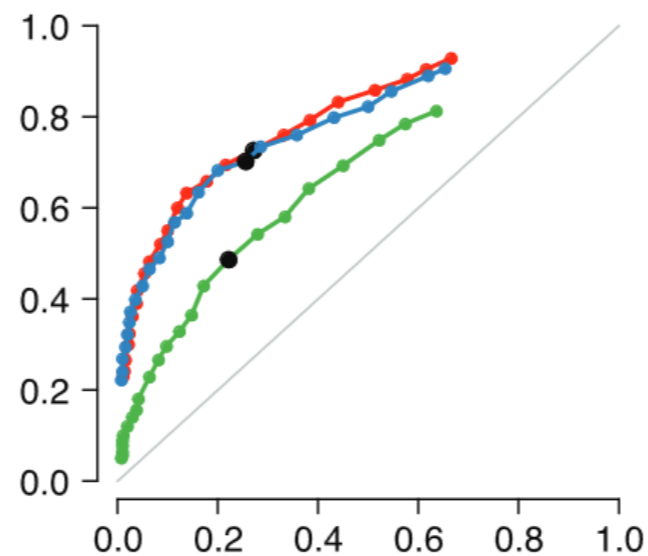
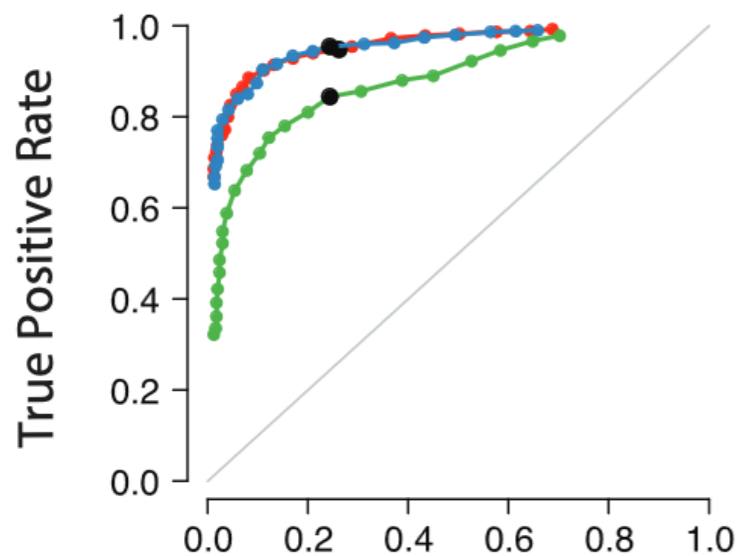
$\sigma_{\varepsilon} = 4$

$\sigma_{\varepsilon} = 6$

$\sigma_{\varepsilon} = 8$



50 Day Transition

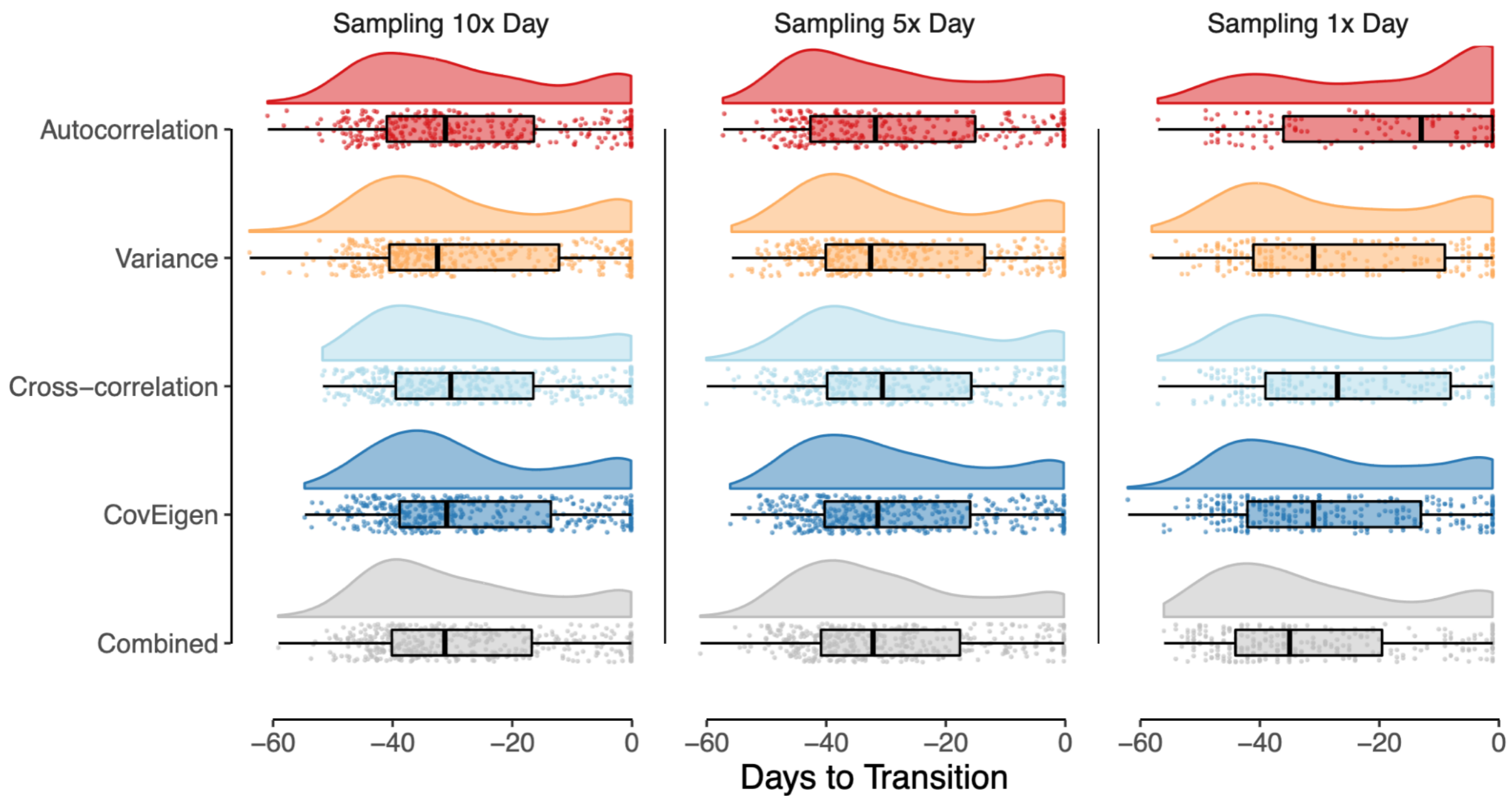


25 Day Transition

False Positive Rate

False Positive Rate


False Positive Rate



Interim conclusion II

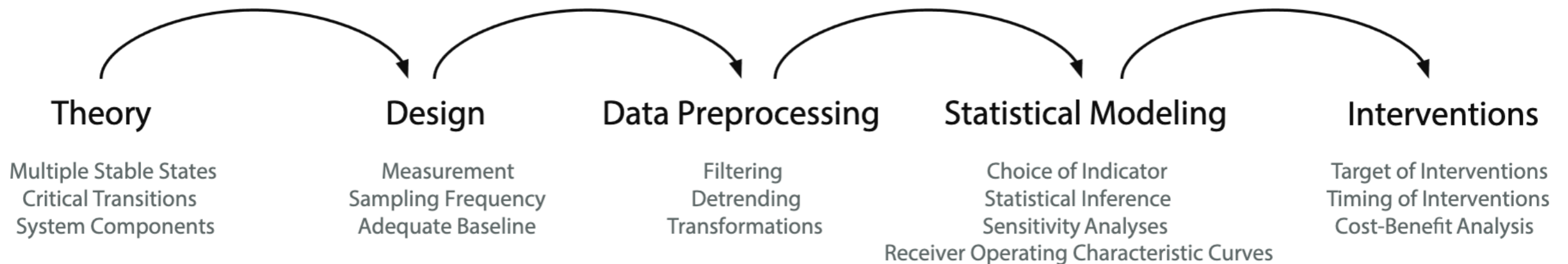
Article | [Open access](#) | Published: 01 December 2023

Early warning signals have limited applicability to empirical lake data

[Duncan A. O'Brien](#) , [Smita Deb](#), [Gideon Gal](#), [Stephen J. Thackeray](#), [Partha S. Dutta](#), [Shin-ichiro S. Matsuzaki](#), [Linda May](#) & [Christopher F. Clements](#)

[Nature Communications](#) **14**, Article number: 7942 (2023) | [Cite this article](#)

- **Even if tipping points exist**, using EWS successfully is very difficult
 - Extent of noise and sampling frequency huge impact on performance
 - Time to transition, extent of baseline, decision threshold, ...
 - Caveat: type of system




Overlapping timescales obscure early warning signals of the second COVID-19 wave

Fabian Dablander¹, Hans Heesterbeek², Denny Borsboom¹ and John M. Drake^{3,4}

¹Department of Psychological Methods, University of Amsterdam, Amsterdam, The Netherlands

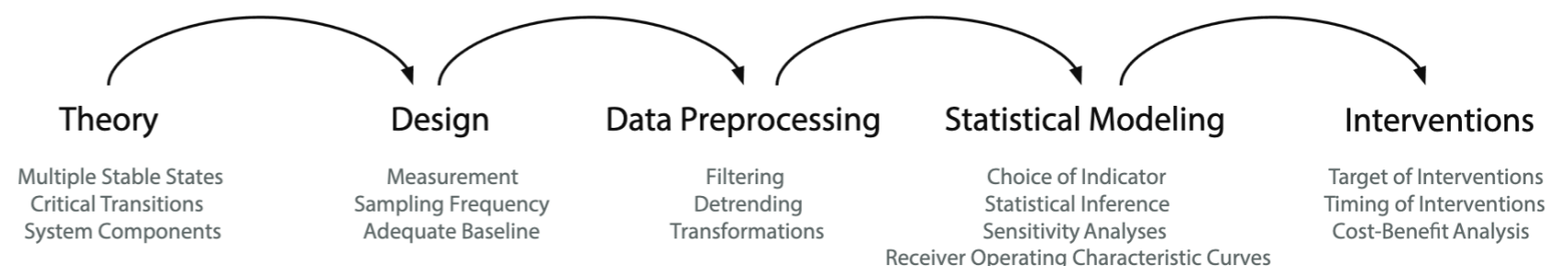
²Department of Population Health Sciences, Utrecht University, Utrecht, The Netherlands

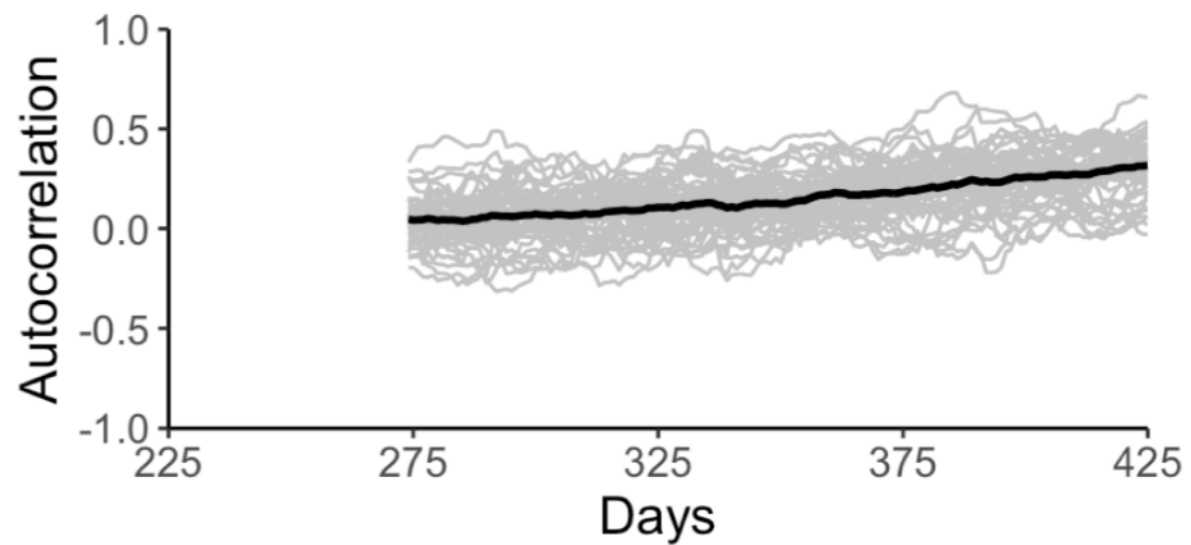
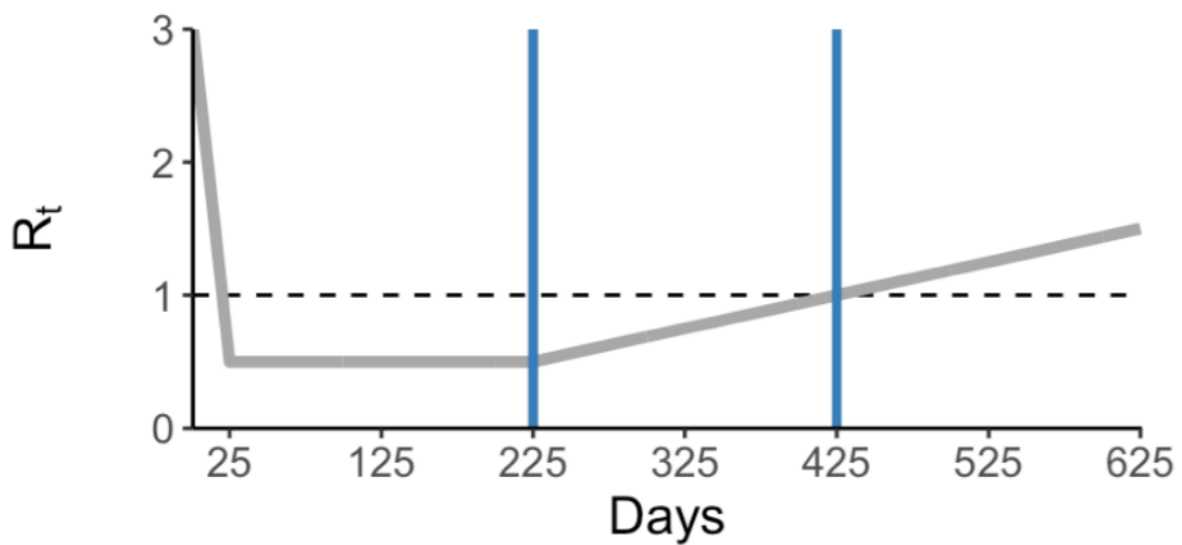
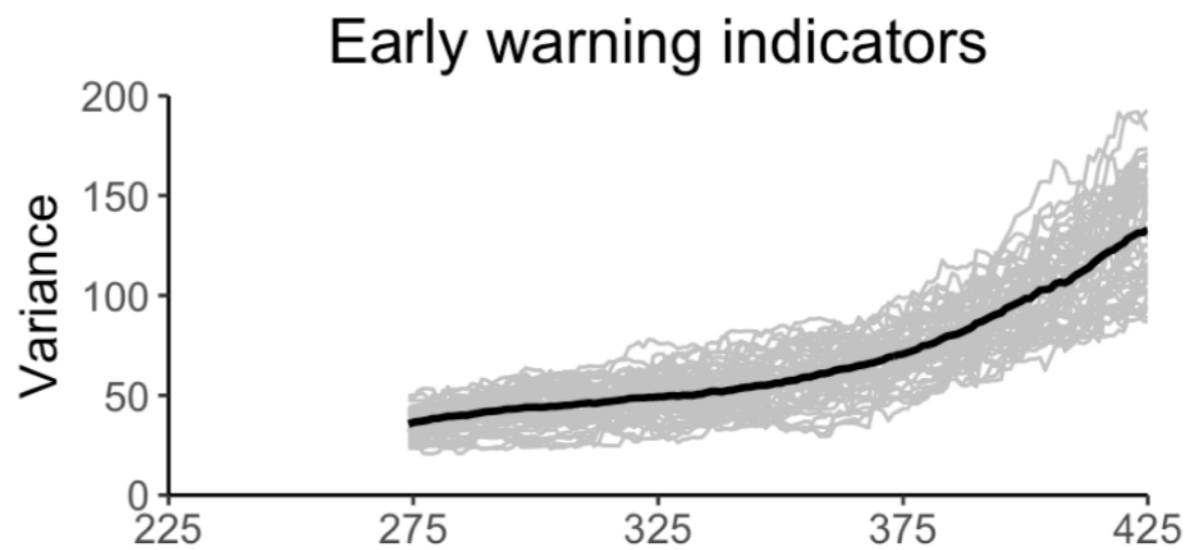
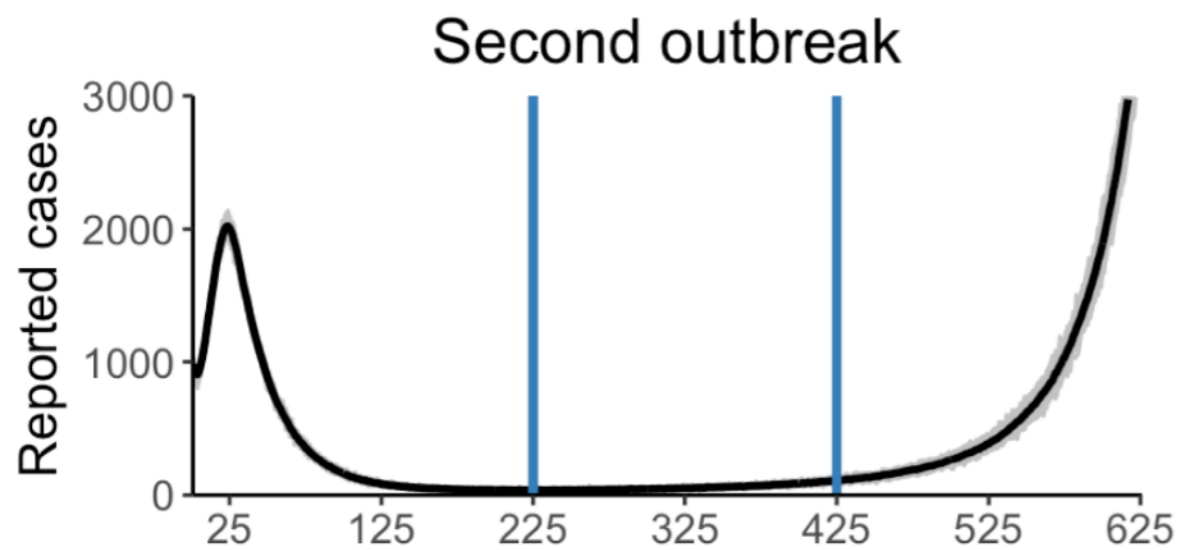
³Odum School of Ecology, and ⁴Center for the Ecology of Infectious Diseases, University of Georgia, Athens, GA, USA

 FD, 0000-0003-2650-6491; JMD, 0000-0003-4646-1235

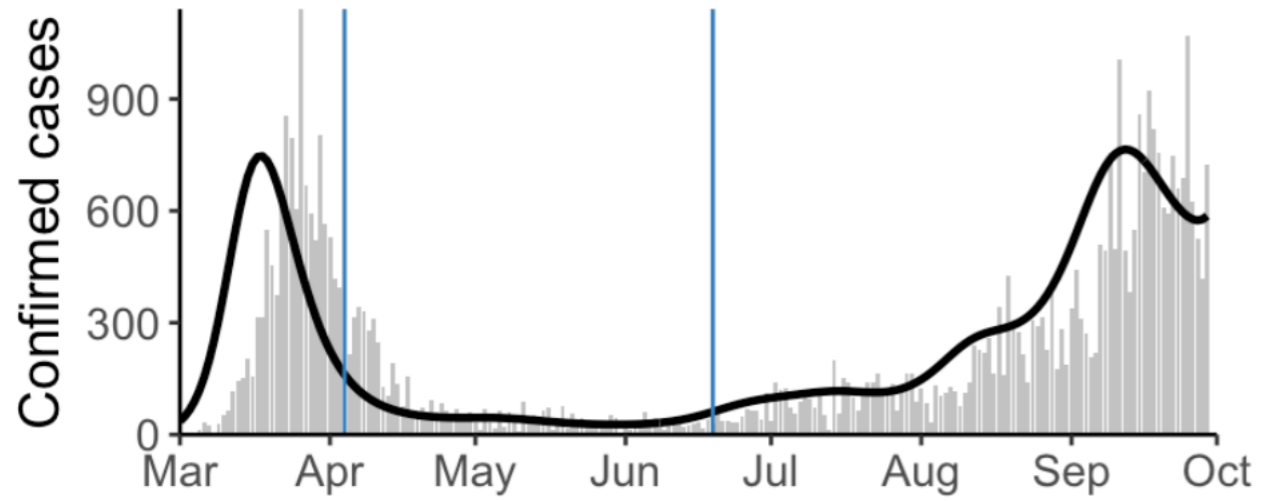
Ahead of the curve

- O'Regan & Drake ([2013](#))
 - Critical slowing down occurs in the basic SIS and SIR compartmental models
- O'Dea et al. ([2018](#))
 - In a SIR model, the autocorrelation of the number of infected provides a better estimate of the distance to the epidemic threshold than the autocorrelation of the number of susceptibles
- Brett et al. ([2018](#))
 - Case reports are lagging behind; deaths lag behind substantially
 - Estimating R_t is extremely difficult
 - Several early warning indicators robust to reporting errors and aggregation in anticipating epidemic transitions
- Brett et al. ([2020](#))
 - Critical slowing down occurs in high-dimensional models

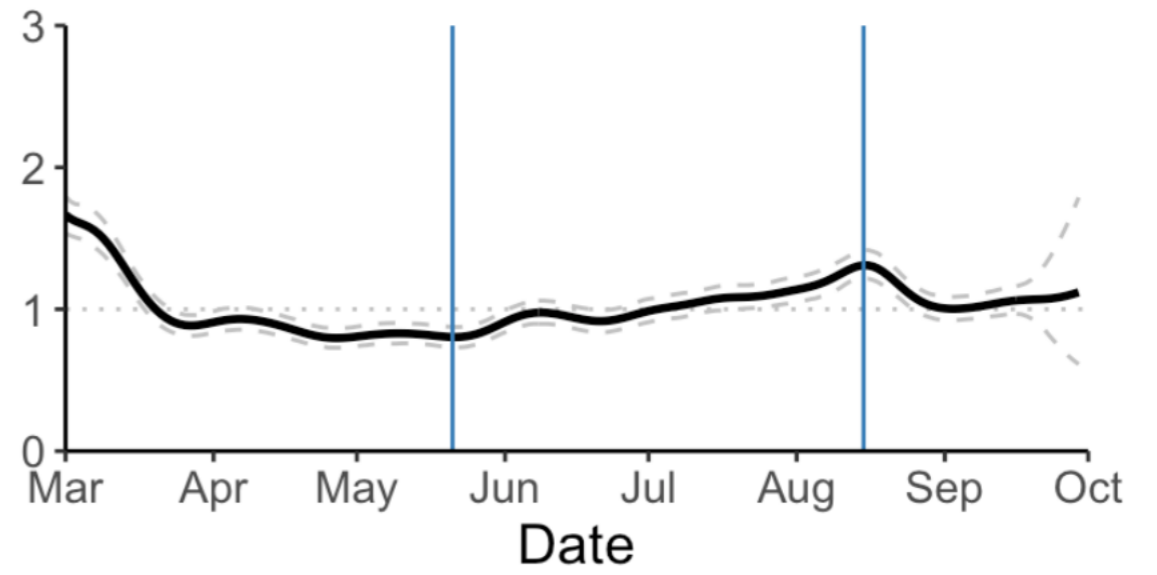
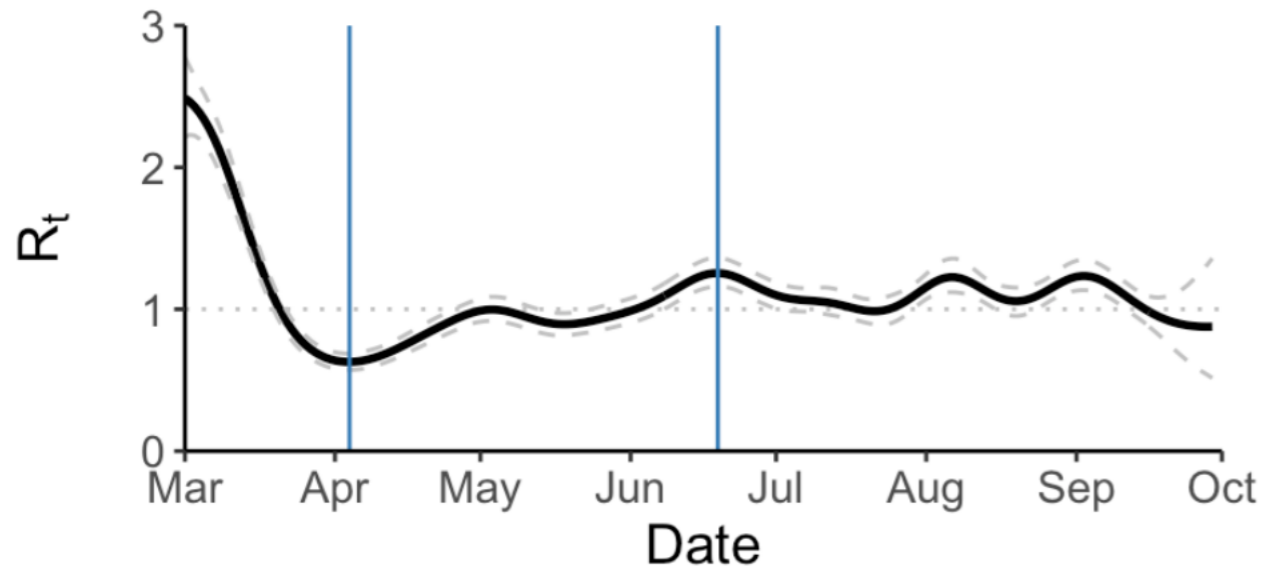
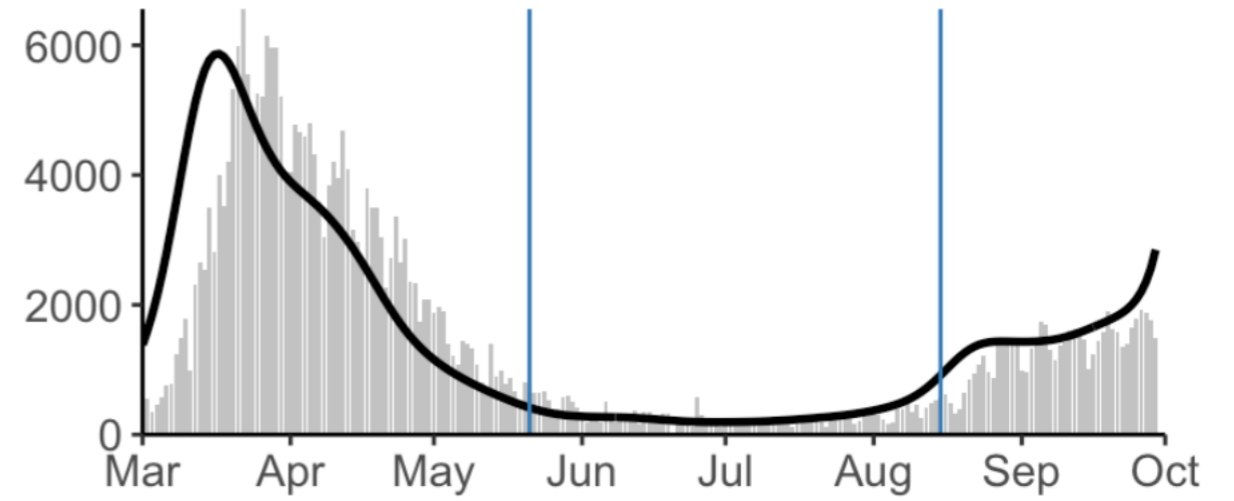


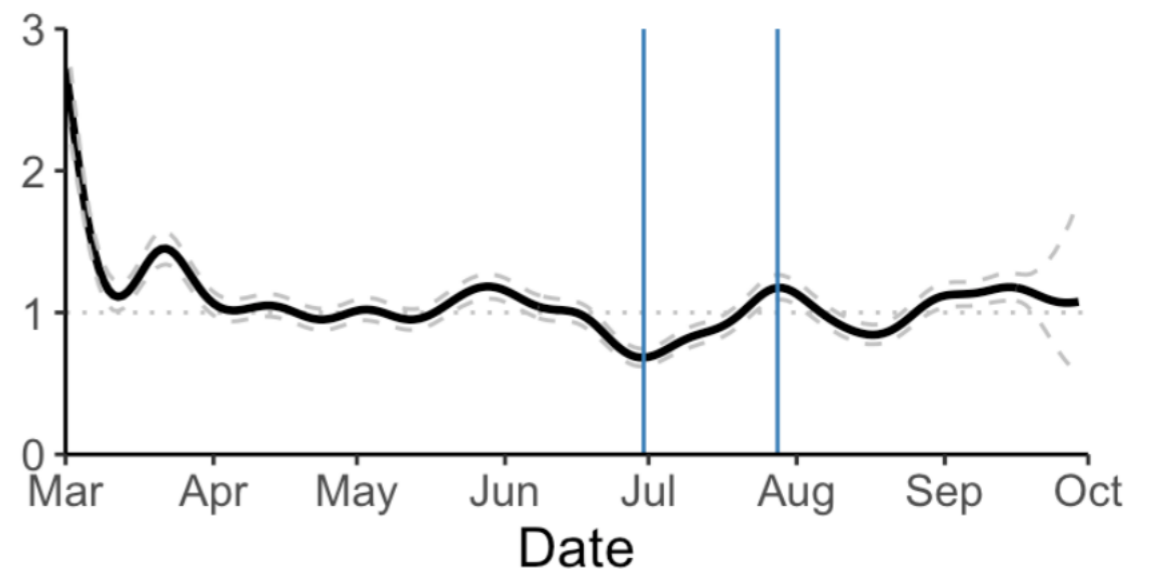
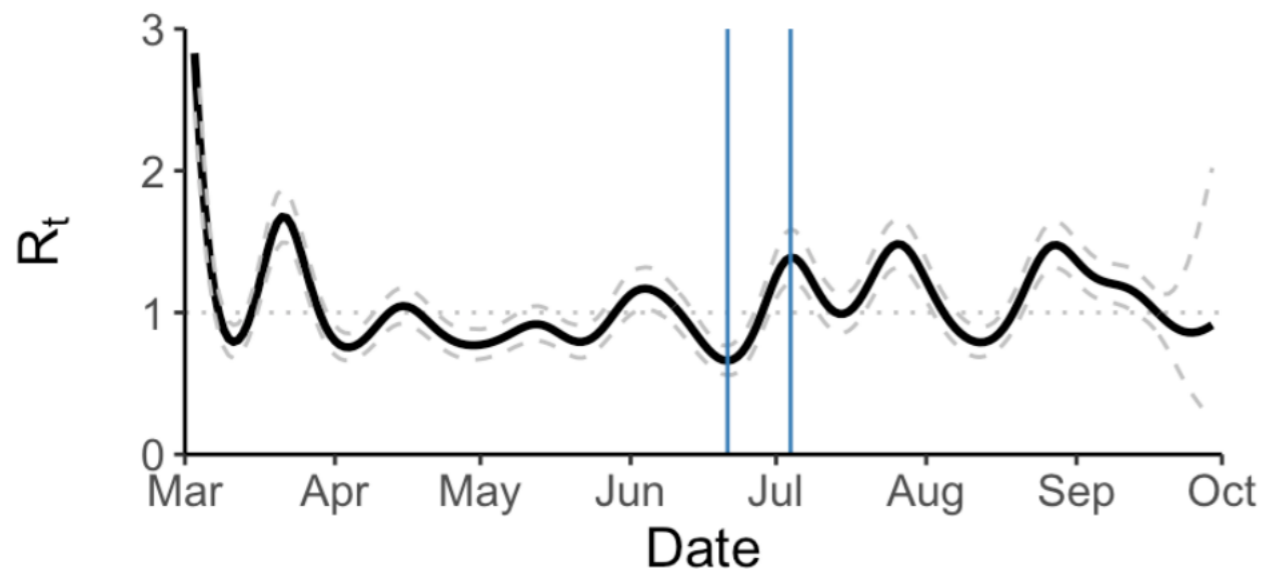
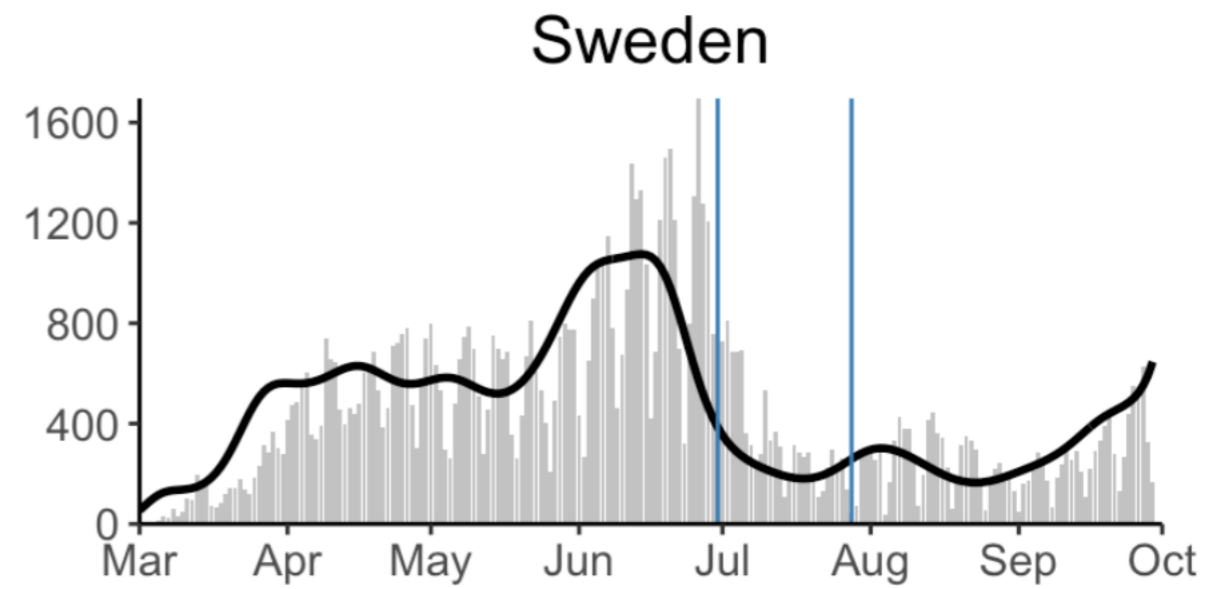
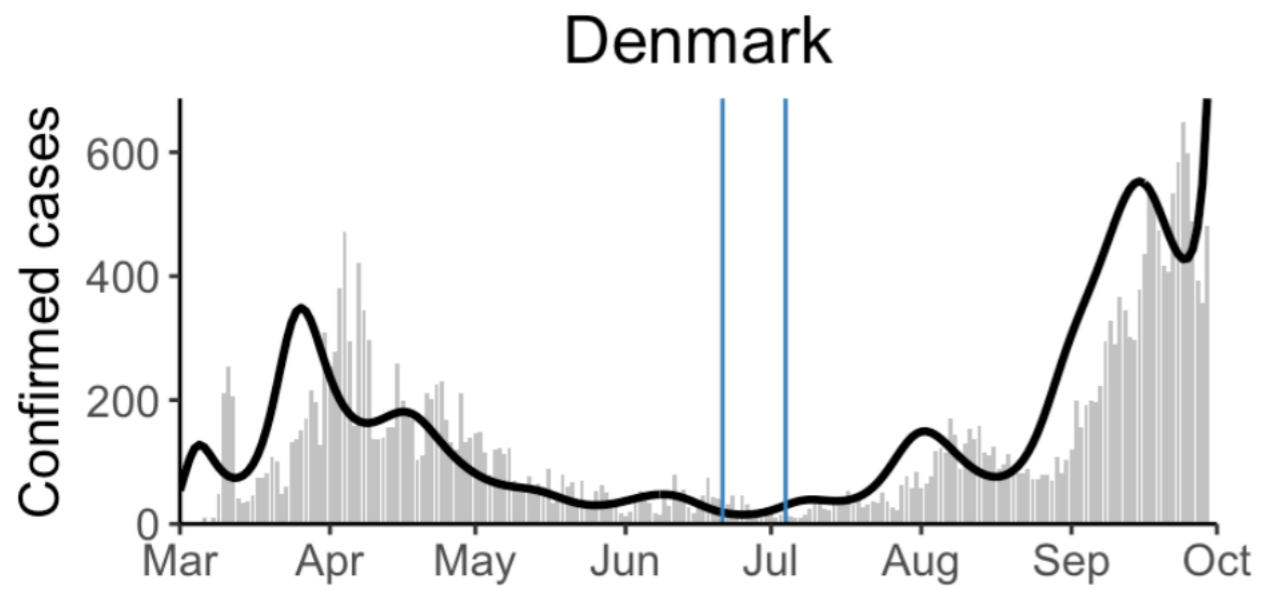


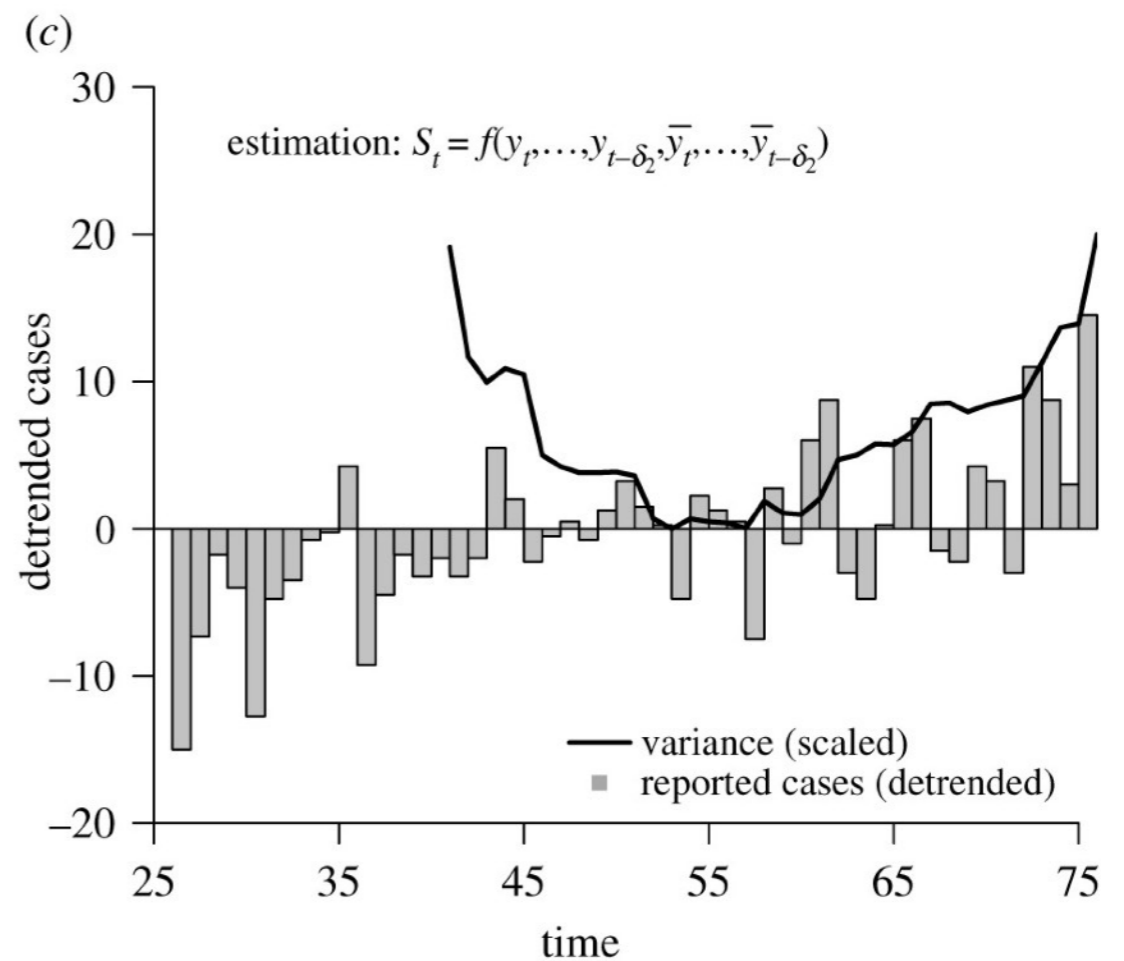
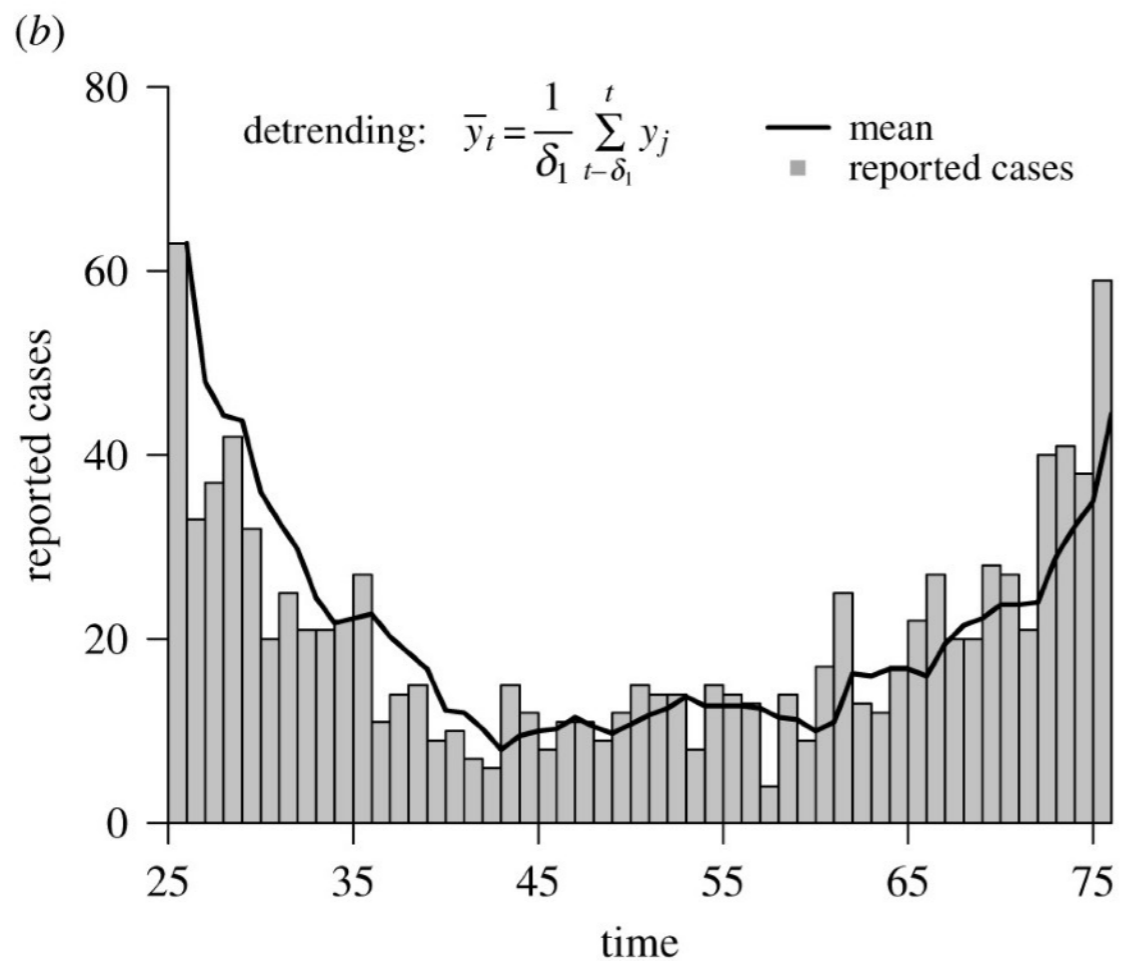
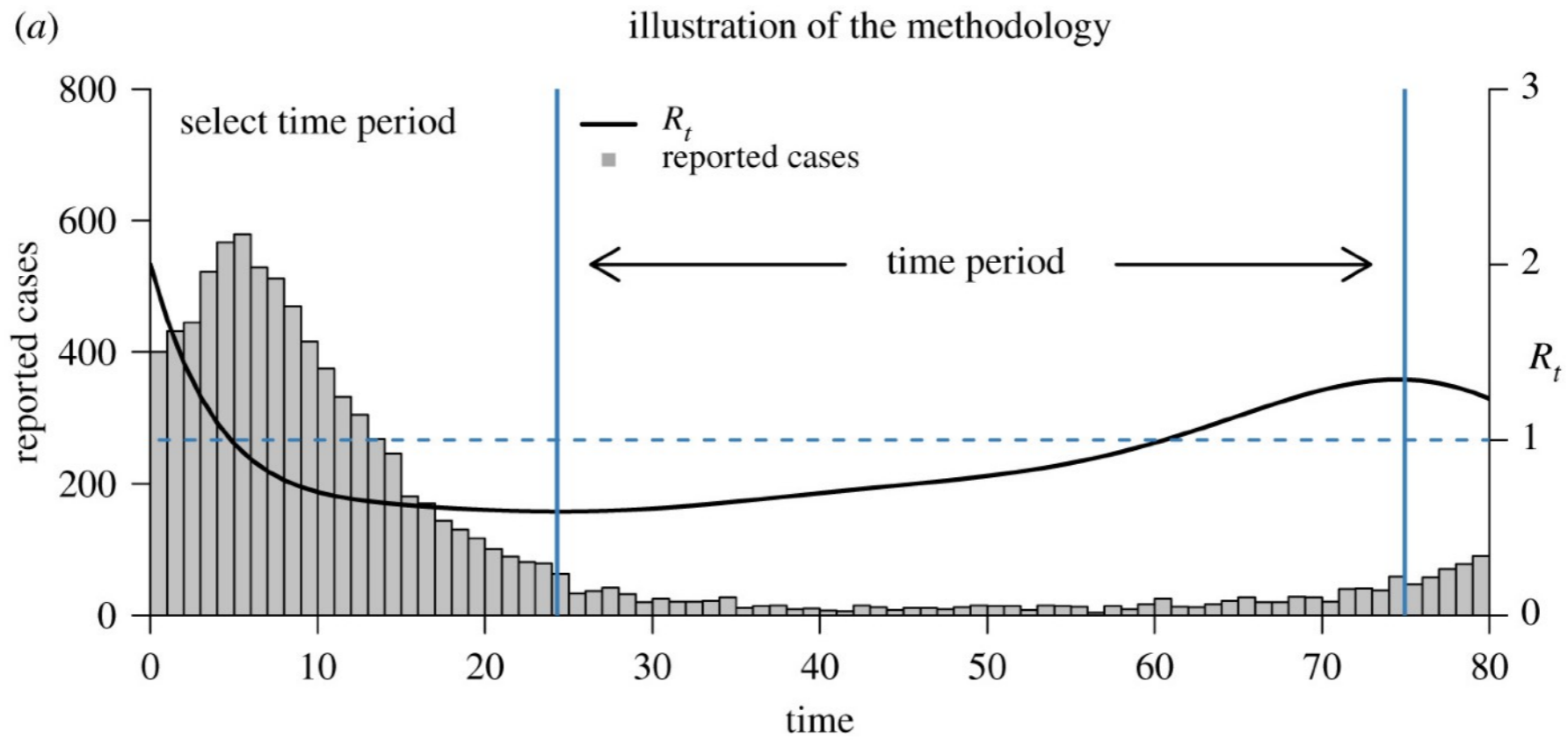
Austria



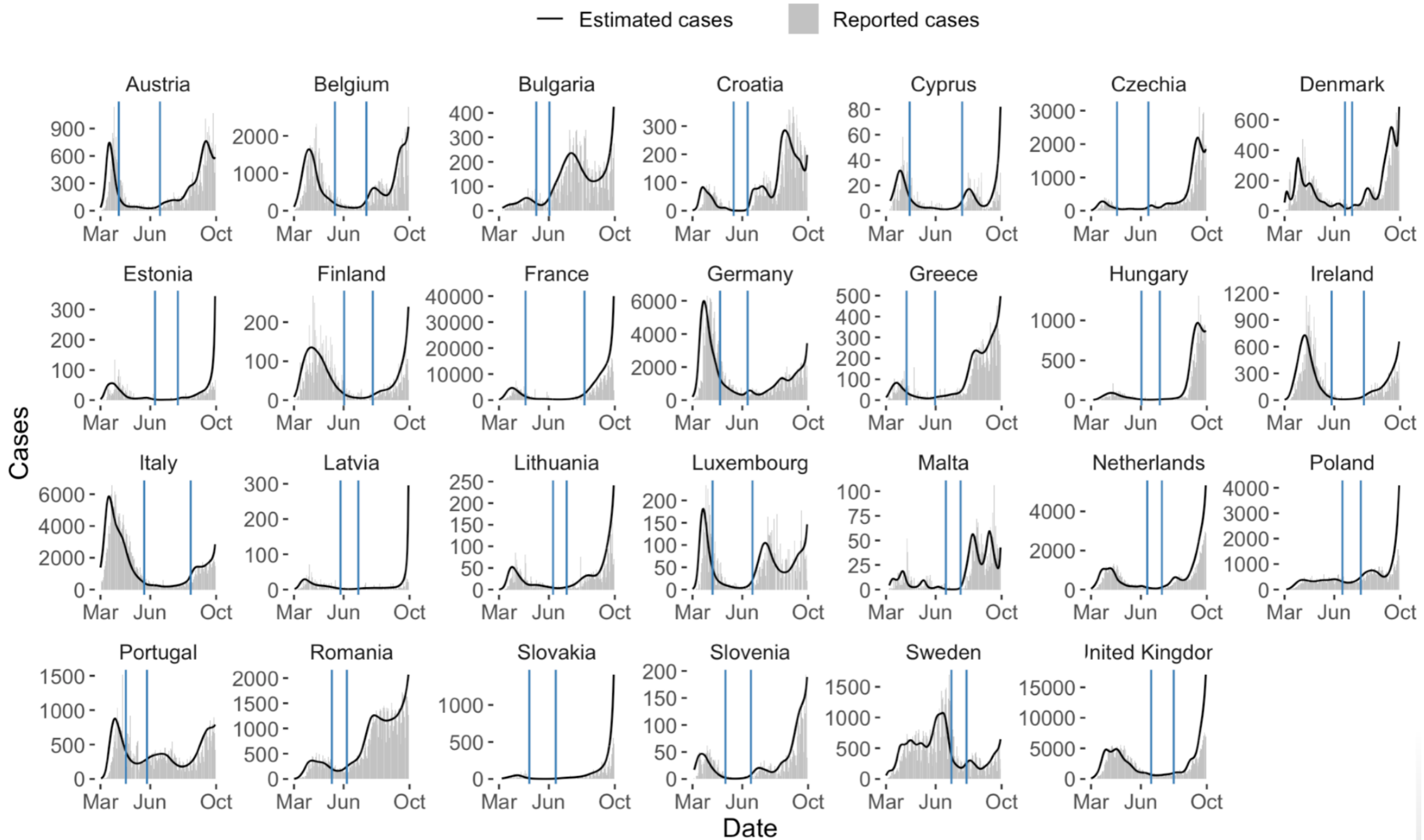
Italy



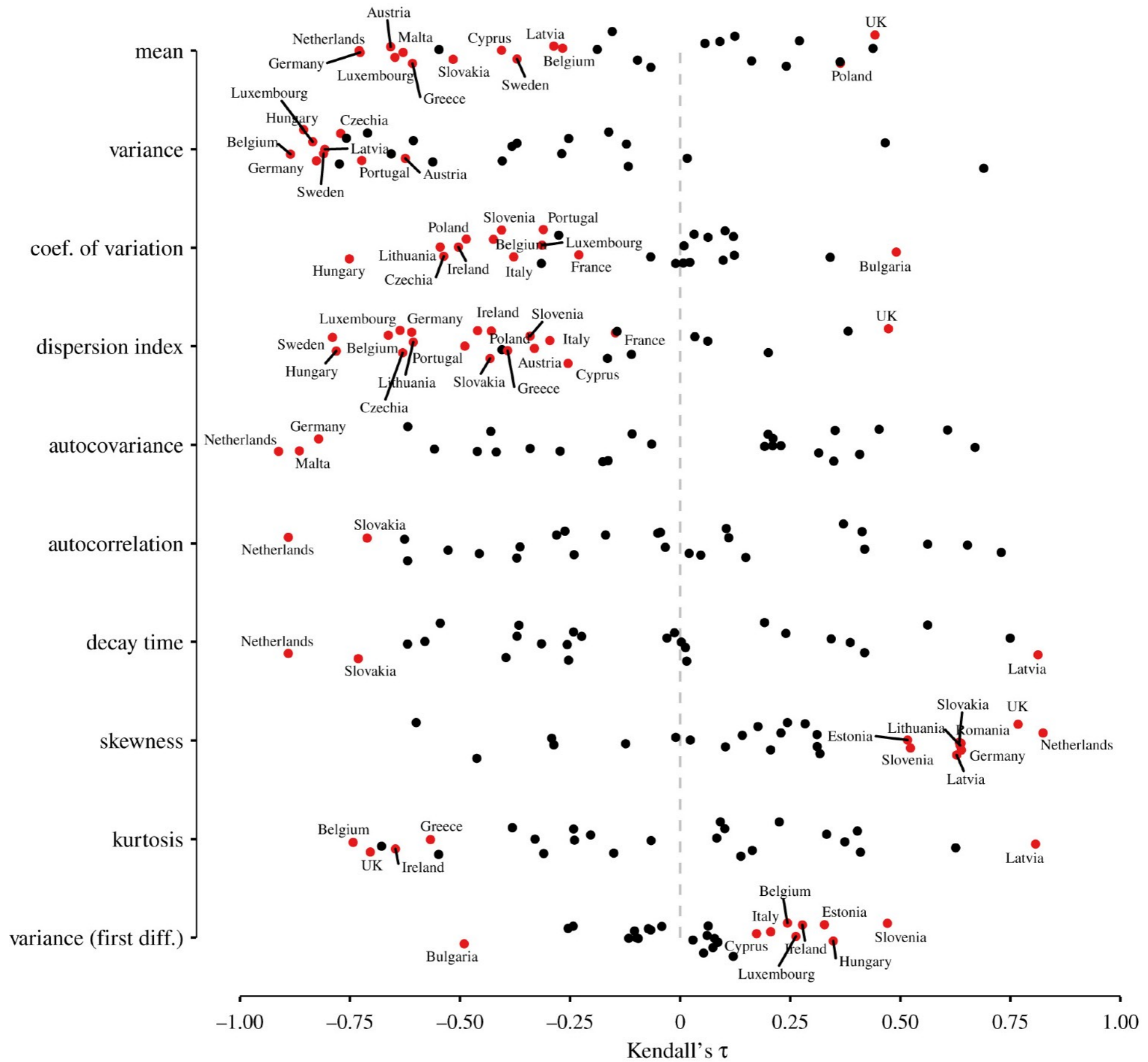


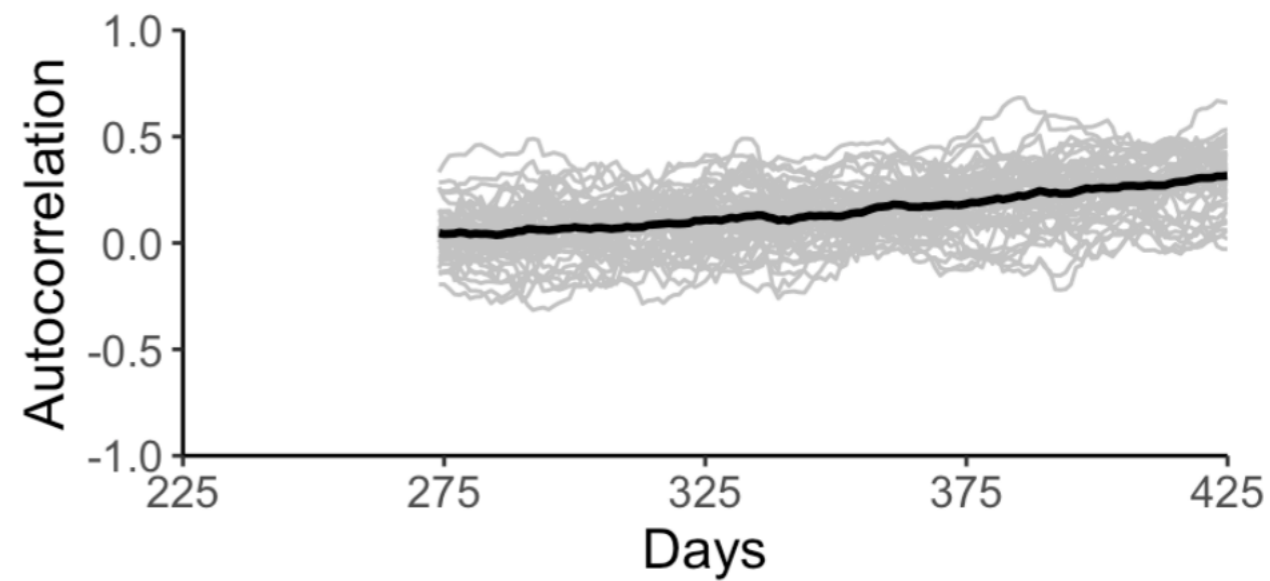
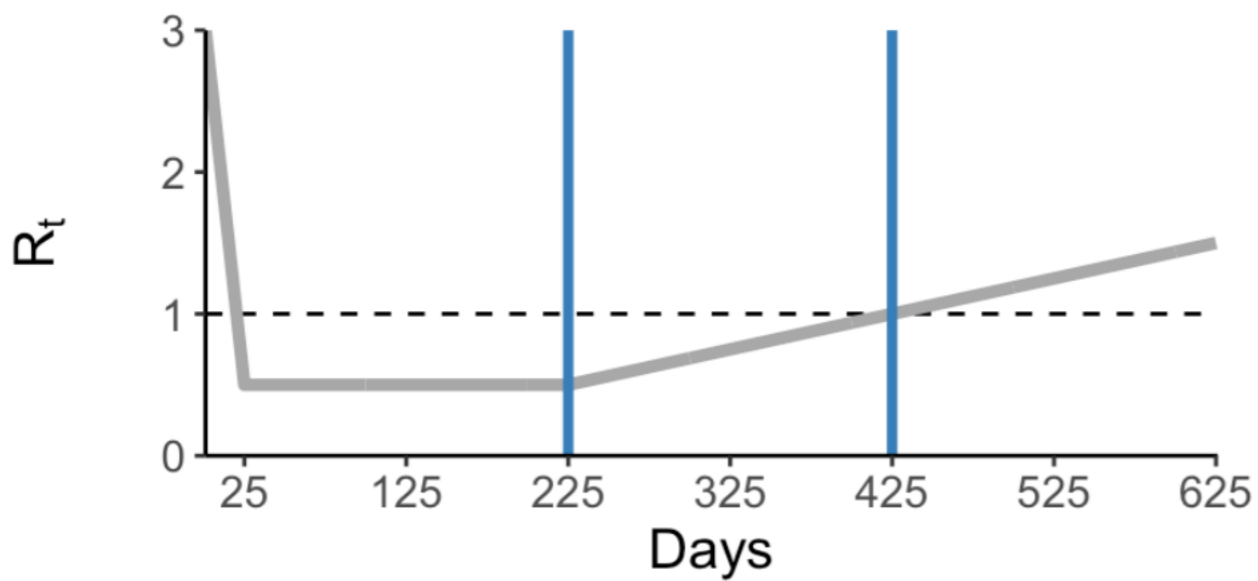
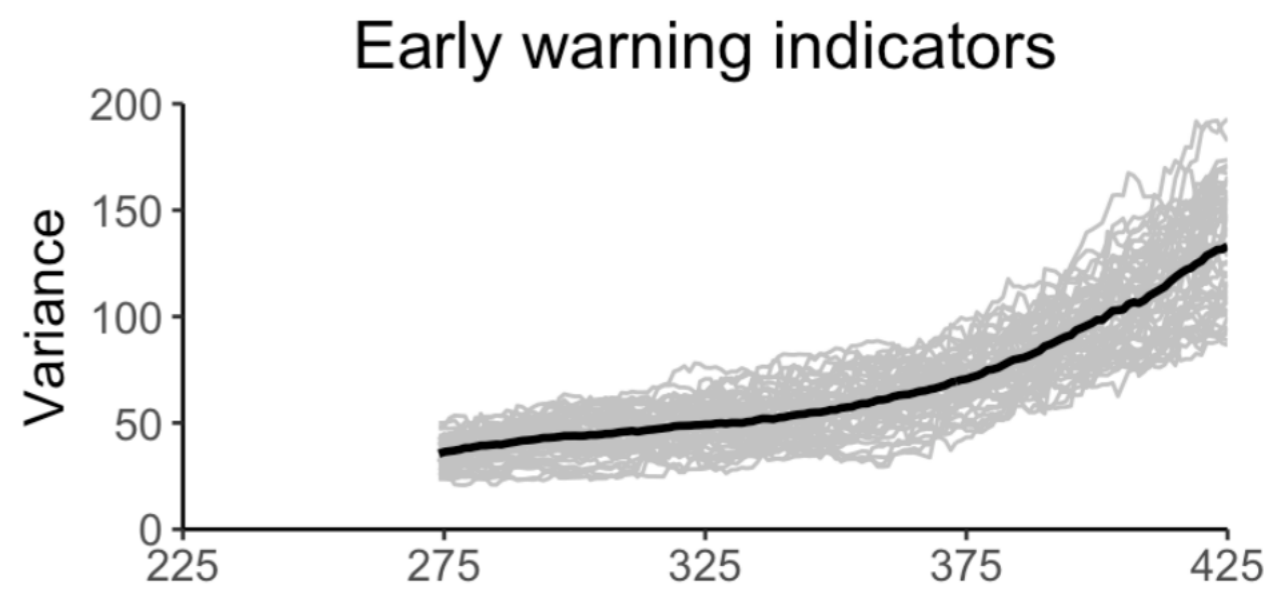
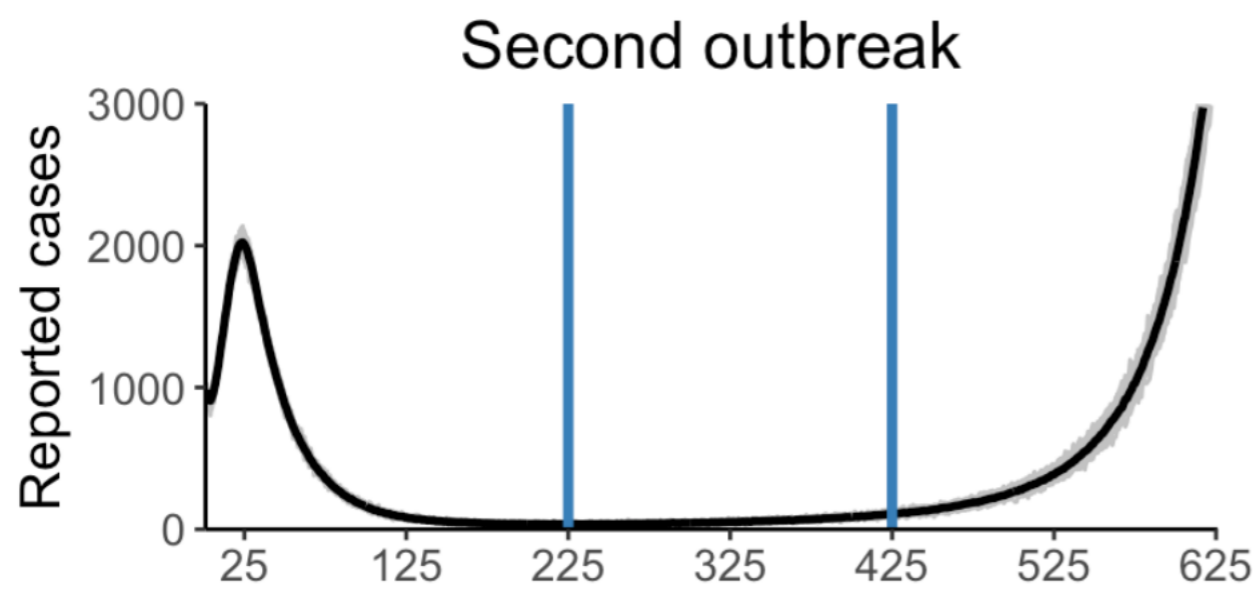


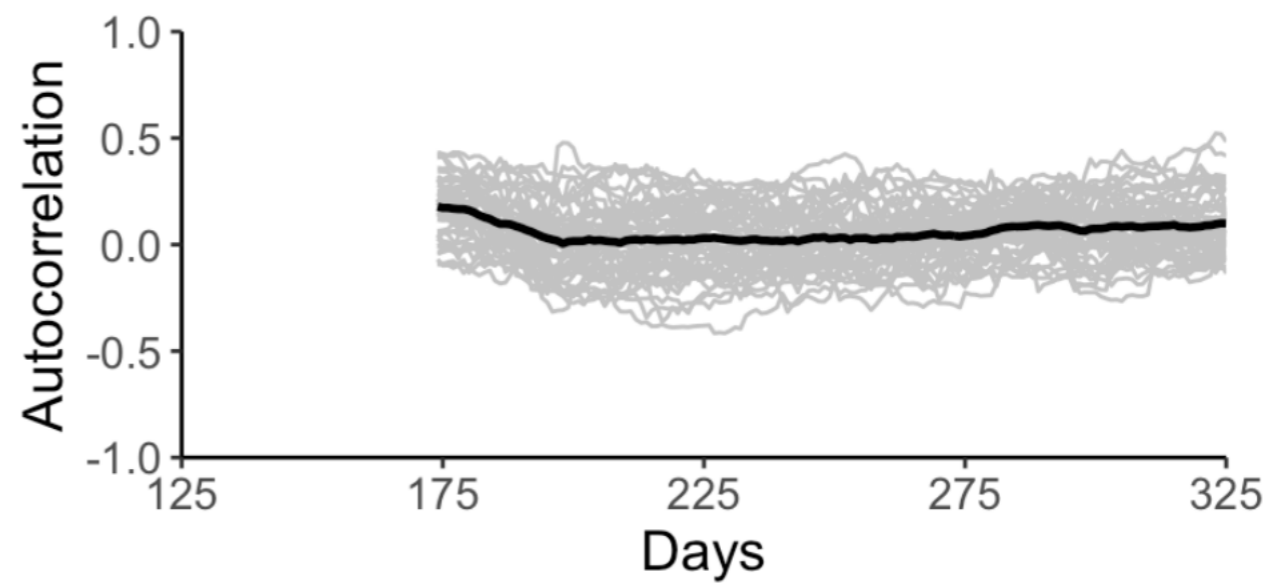
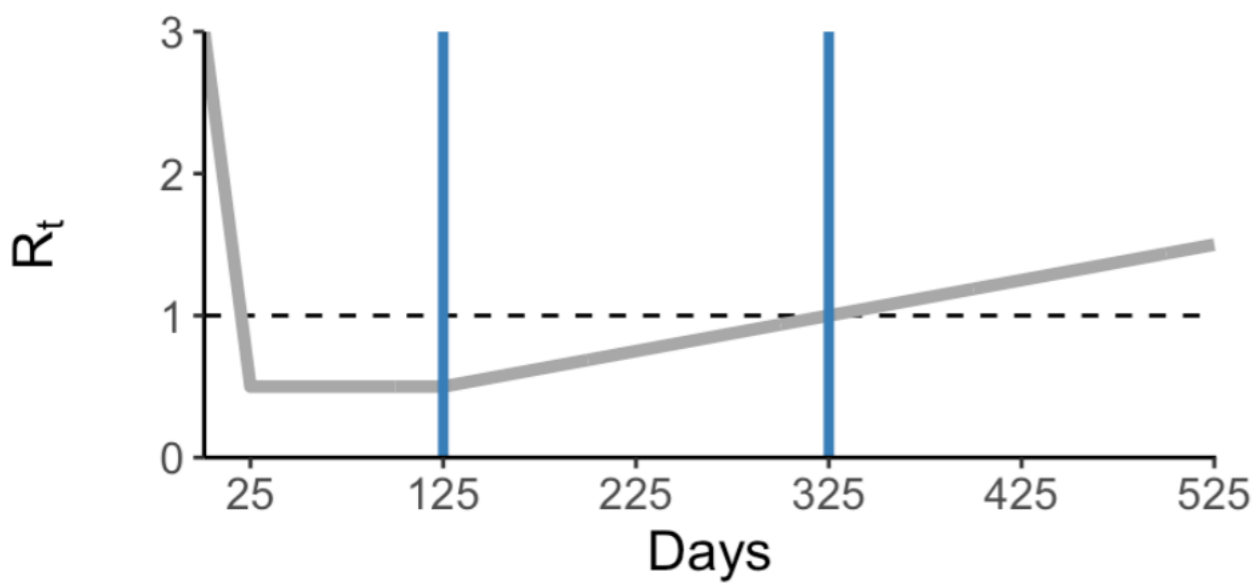
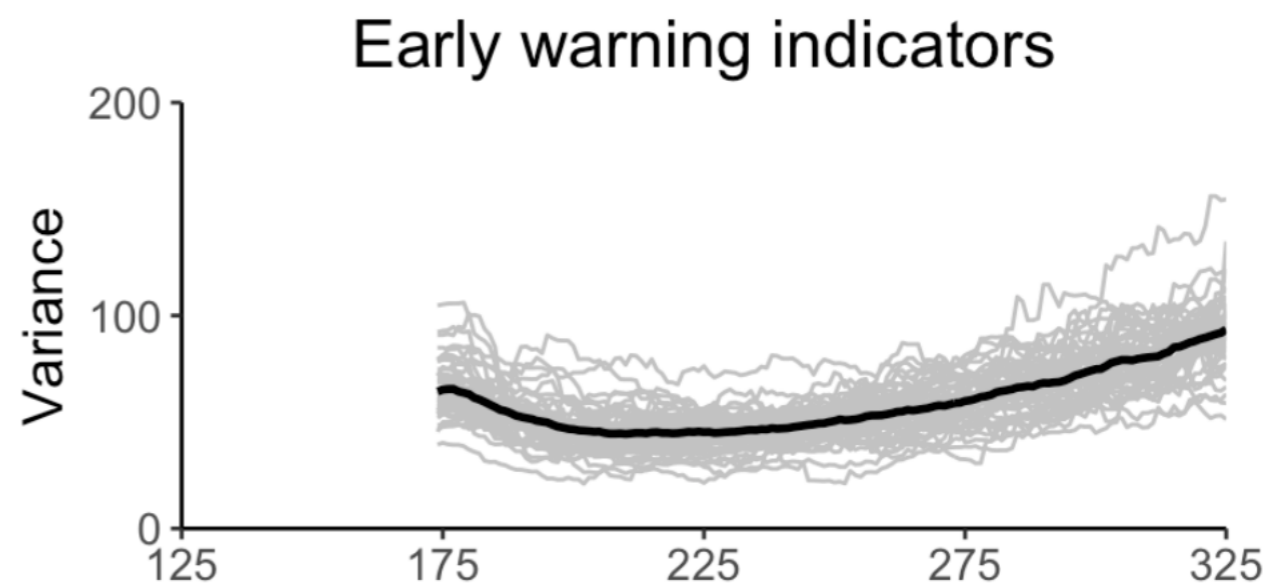
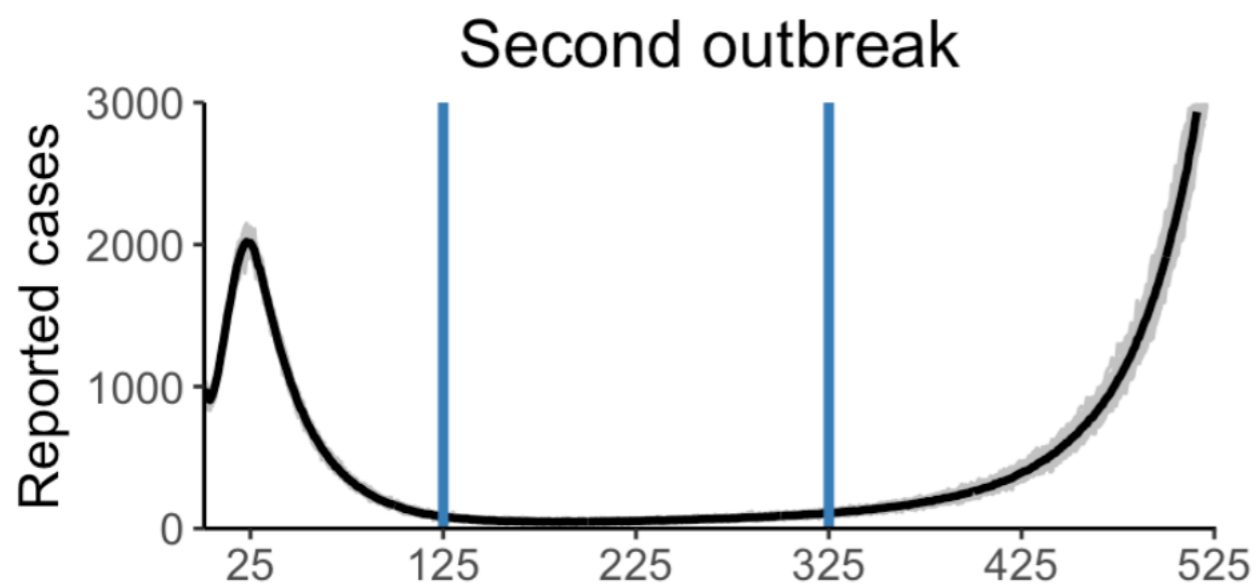
Reported and estimated COVID-19 cases in Europe

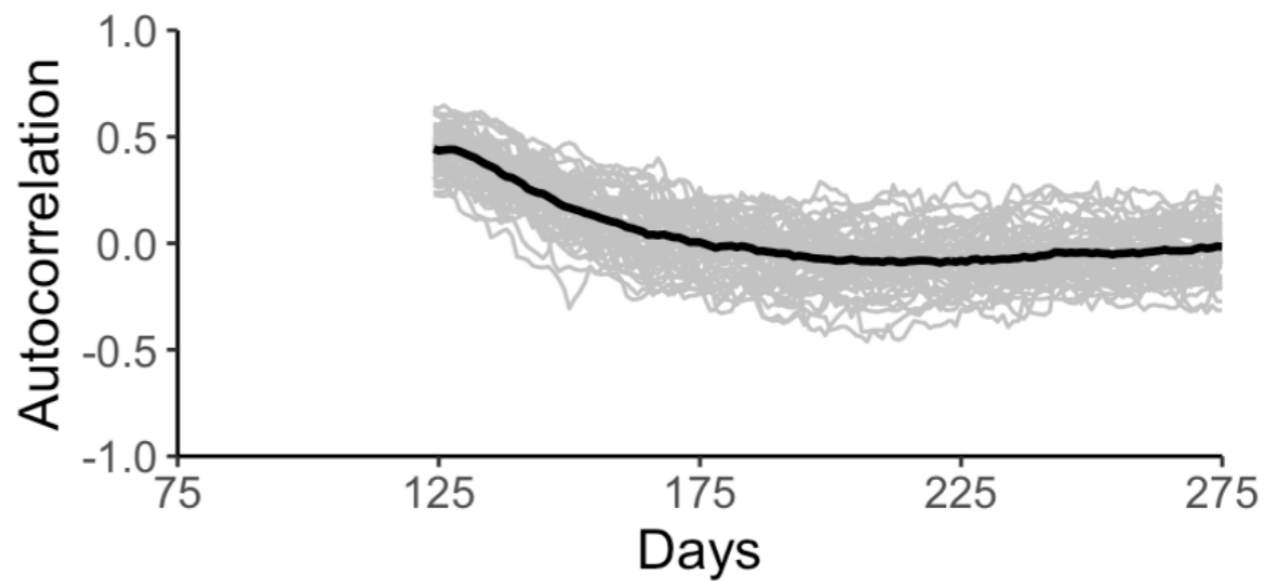
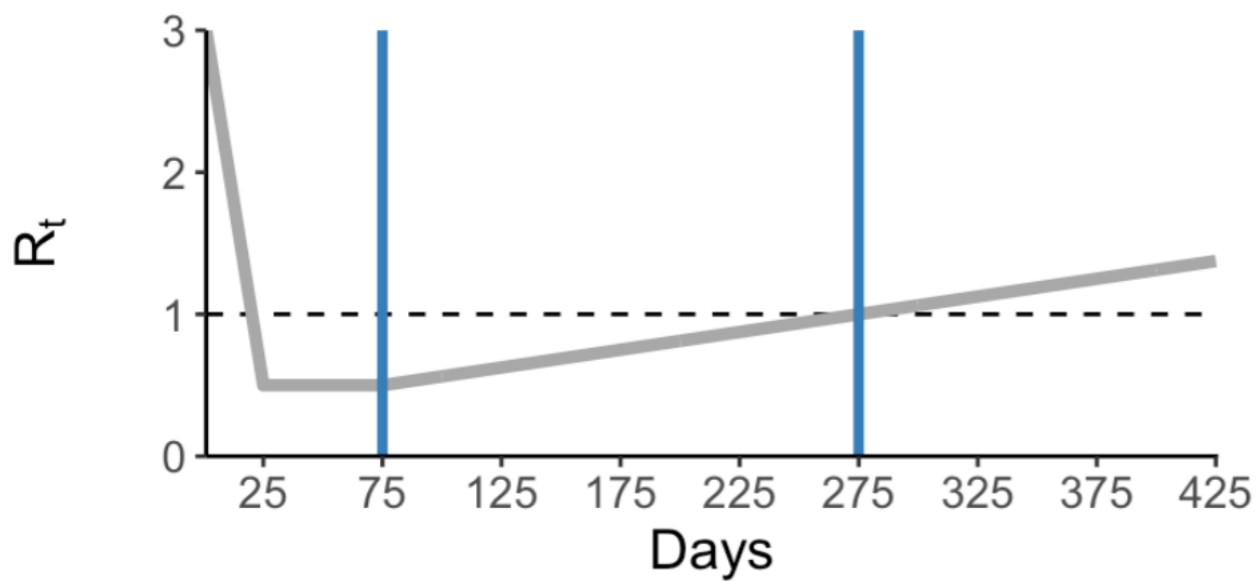
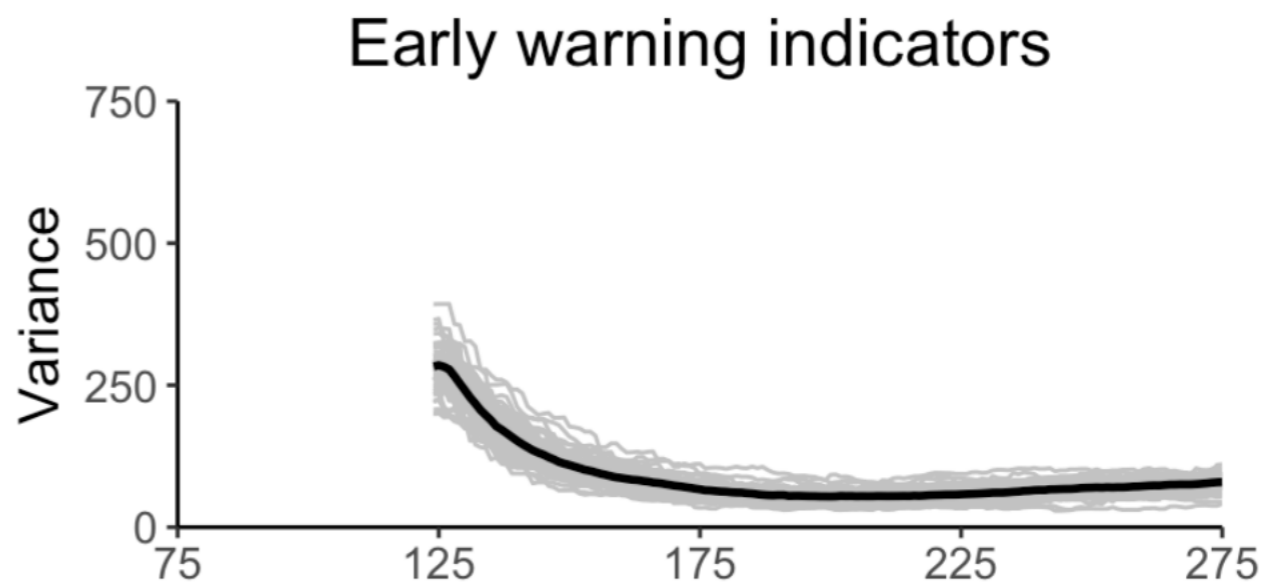
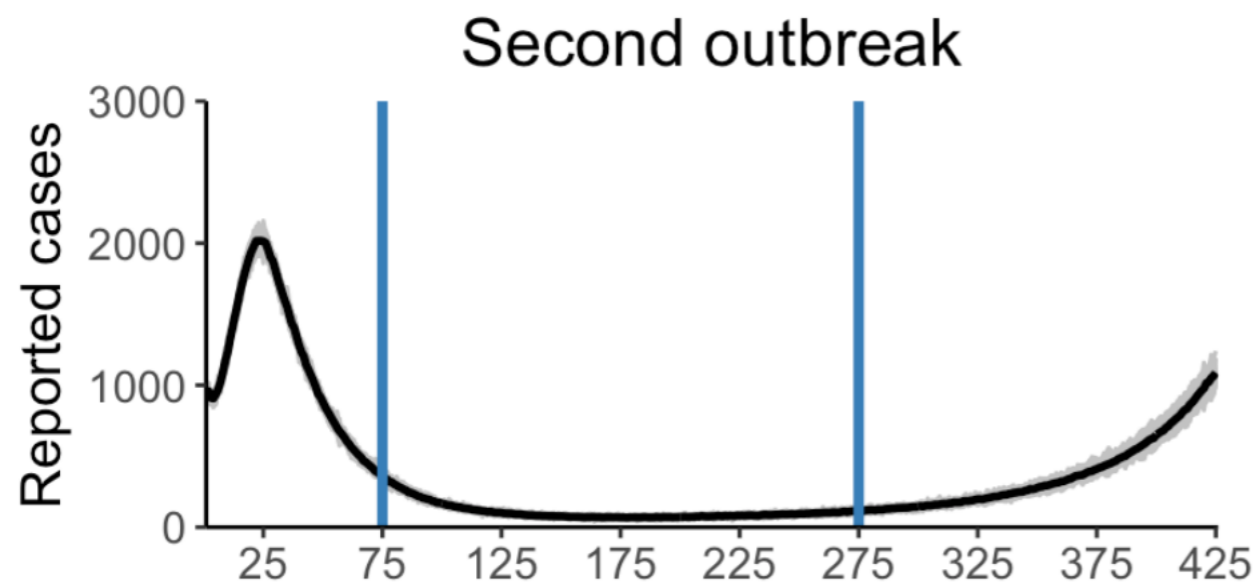


Kendall's τ for early warning indicators across countries



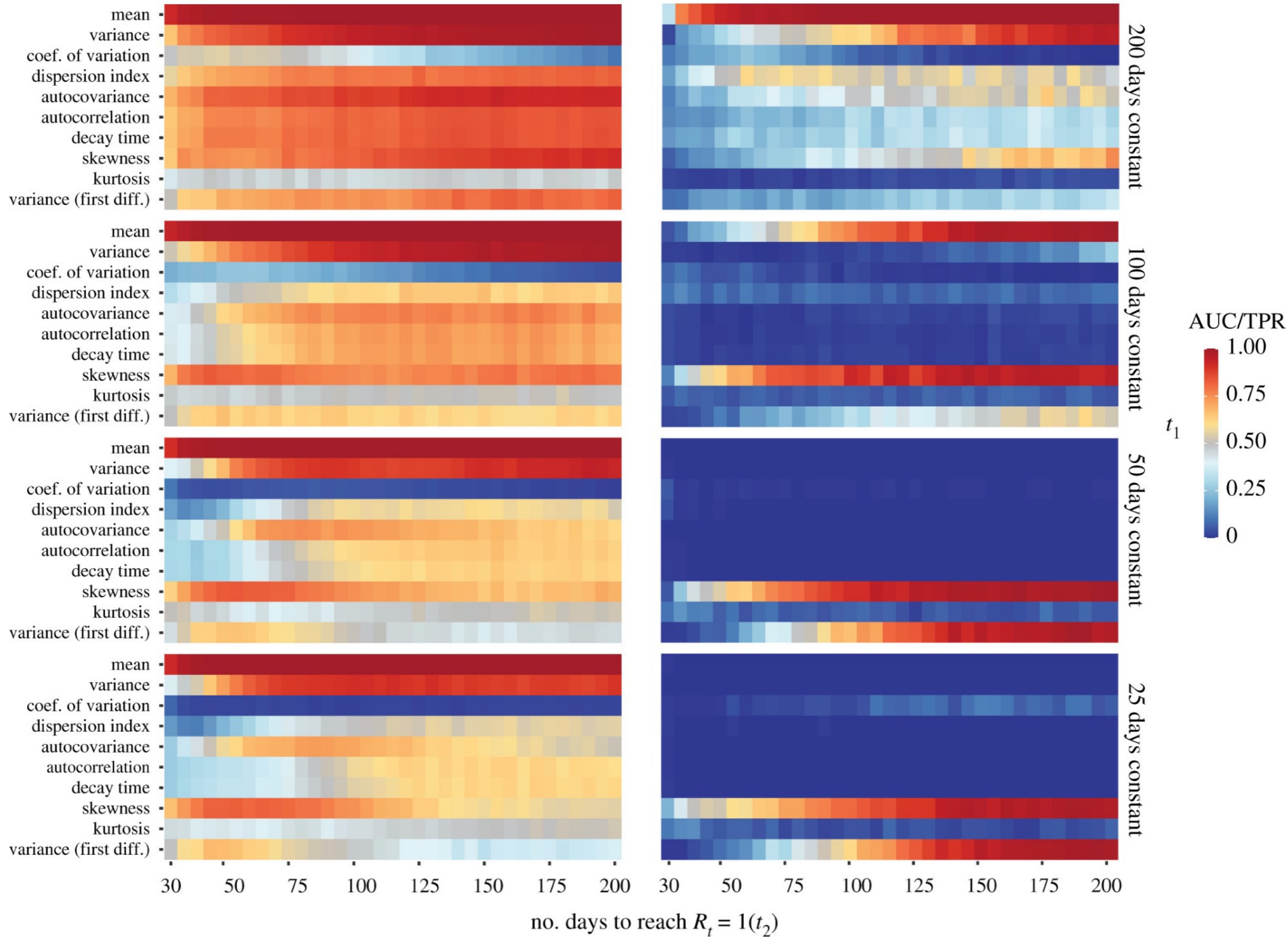






area under the curve (a)

true positive rate (b)

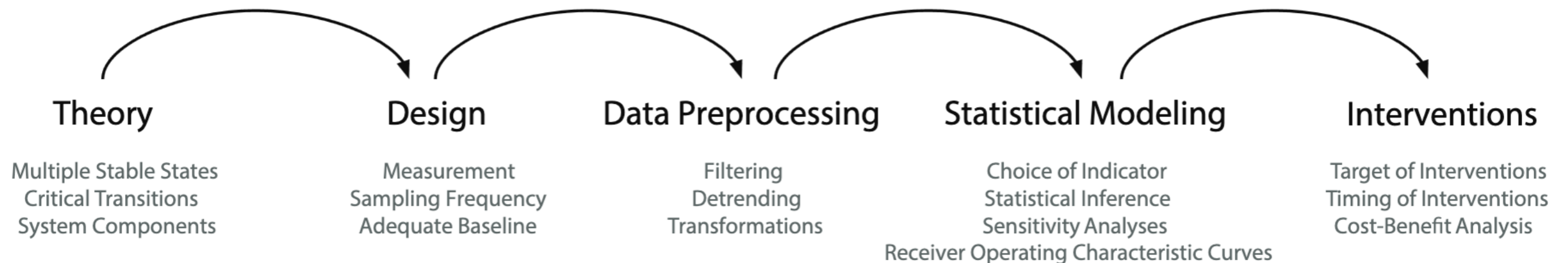


Interim conclusion III

- Indicators did not reliably rise prior to the 2nd COVID-19 wave
 - In fact, they tended to *decrease* rather than *increase*
 - This is due to the persistent transient of the first wave
 - Assumption of slow forcing critical
- Theoretical understanding helped to make sense of “peculiar” patterns
- Even if indicators would reliably rise, many practical challenges remain
- For details, see Dablander, Heesterbeek, Borsboom, & Drake ([2022](#))

Conclusion I


- **Allure of generic early warning signals may have led some fields astray (again)**
- **Successfully applying EWS in practice requires a good understanding of the system**
 - Type of bifurcation, linear / nonlinear driver, timescales, measurement, system components, type of noise, ...
 - Dampen enthusiasm for “softer” sciences and social tipping points



Conclusion II

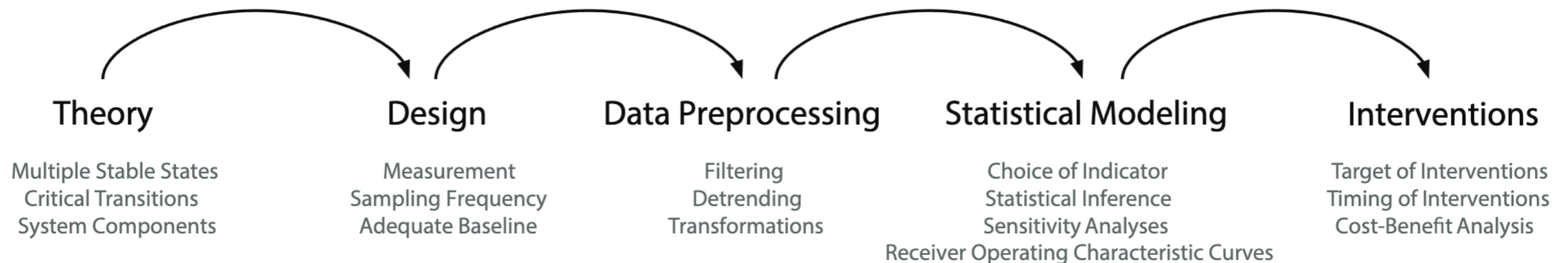
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- **Even with a good understanding, statistical challenges remain tough**
 - Distinguish the bifurcation type promising (Bury et al, Grziwotz et al)
 - Move towards more general prediction tools? (Boettiger & Hastings, 2013)
- **Lots of EWS research – but remains mostly an “intellectual” exercise?**



Thank you!